

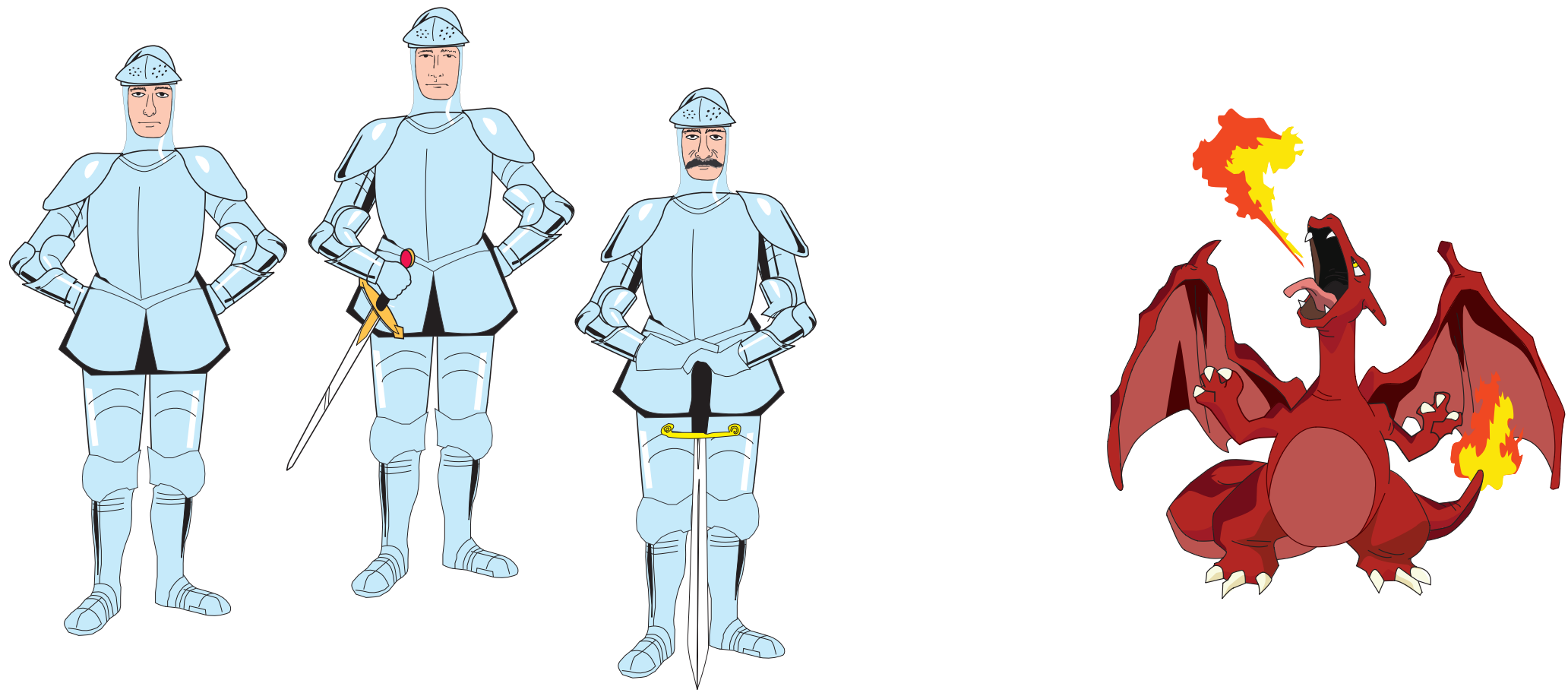
# Achieving Security Despite Compromise Using Zero-knowledge

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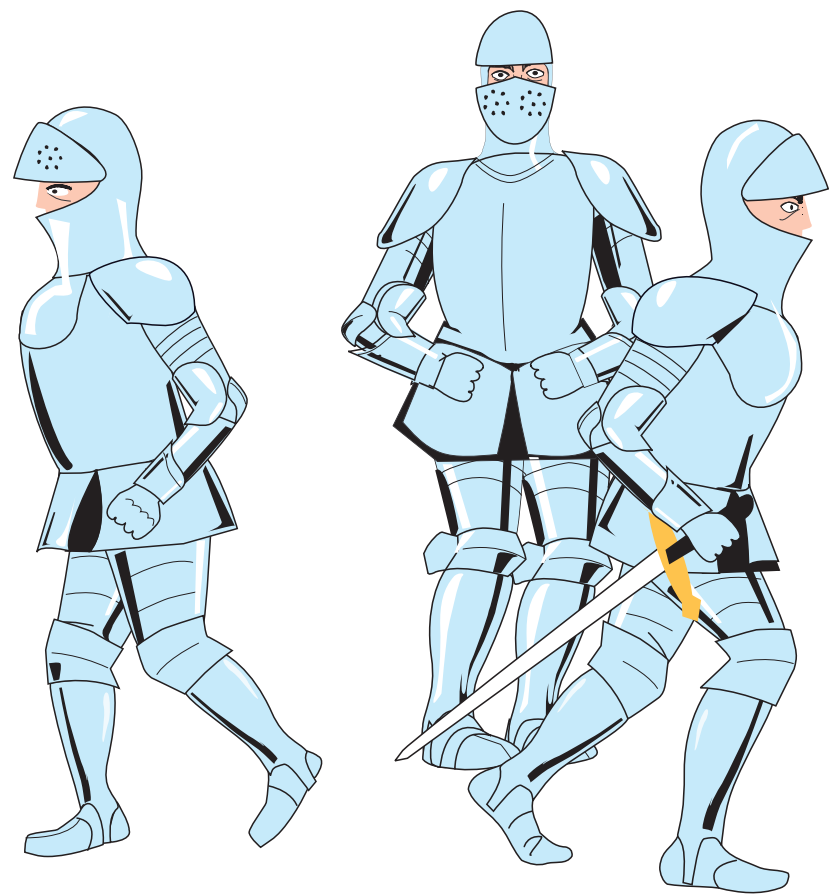
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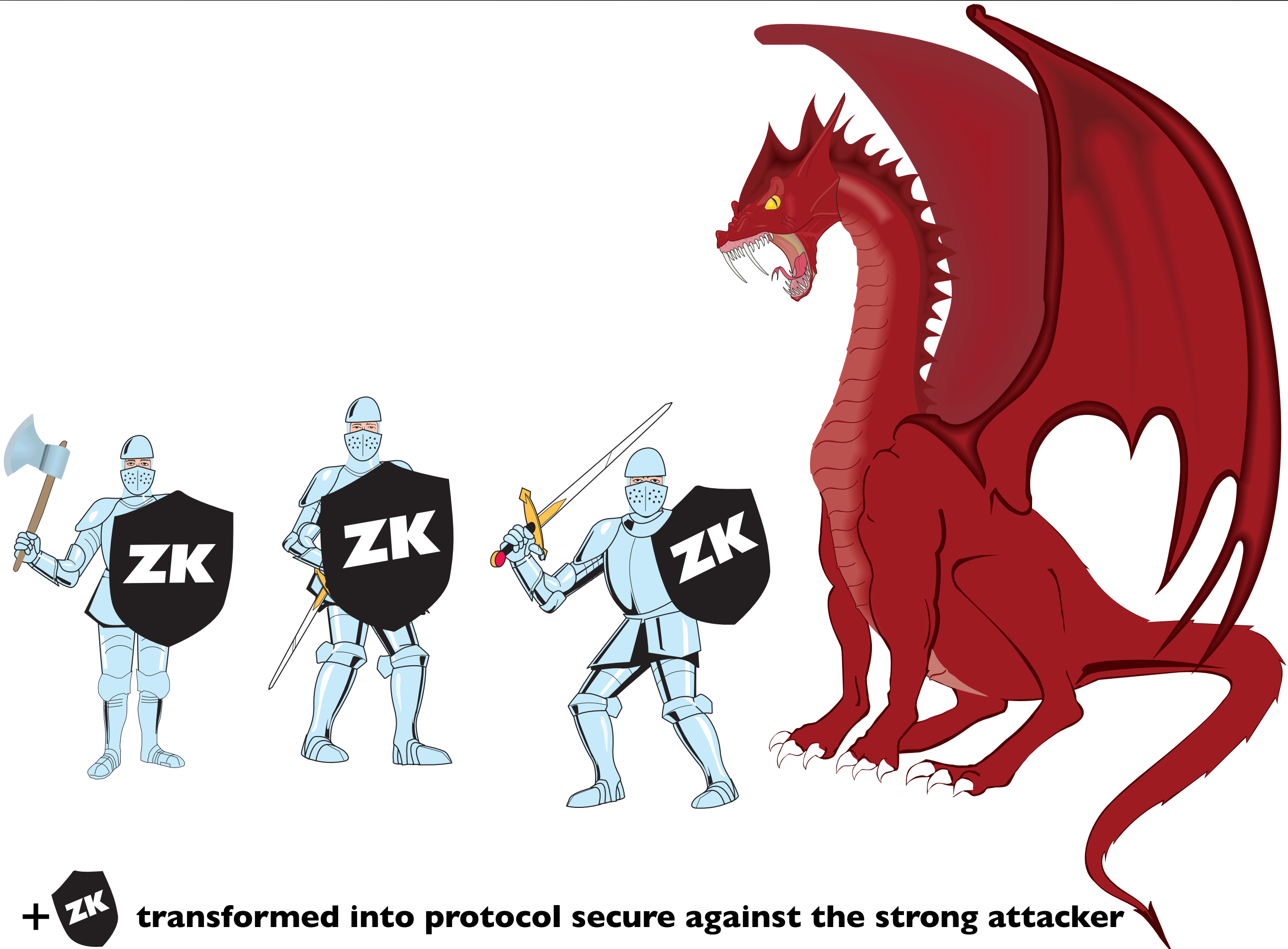
Joint work with: Michael Backes, Martin Grochulla and Matteo Maffei



**protocol secure against a weak attacker**



**but insecure against strong attacker**



+  transformed into protocol secure against the strong attacker



# Contributions

- **Goal:** to aid secure protocol design
  - designer only needs to consider restricted security threats

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- **Goal:** to aid secure protocol design
  - designer only needs to consider restricted security threats
- Automatic protocol transformation adding ZK proofs
  - Enforce authenticity even if participants compromised
  - Preserve secrecy if everybody is honest



# Contributions

- **Goal:** to aid secure protocol design
  - designer only needs to consider restricted security threats
- Automatic protocol transformation adding ZK proofs
  - Enforce authenticity even if participants compromised
  - Preserve secrecy if everybody is honest



**designer can assume attacker cannot compromise participants (easier)**

# Contributions

- **Goal:** to aid secure protocol design
  - designer only needs to consider restricted security threats
- Automatic protocol transformation adding ZK proofs
  - Enforce authenticity even if participants compromised
  - Preserve secrecy if everybody is honest



**transformed protocol secure against attacker that can compromise**

# Contributions

- **Goal:** to aid secure protocol design
  - designer only needs to consider restricted security threats
- Automatic protocol transformation adding ZK proofs
  - Enforce authenticity even if participants compromised
  - Preserve secrecy if everybody is honest
- Automatic verification of the generated protocols
  - We use type system for ZK [Backes, Hritcu & Maffei, CCS '08]
    - now extended to handle security despite compromise



# Contributions

- **Goal:** to aid secure protocol design and implementation
  - designer only needs to consider restricted security threats
- Automatic protocol transformation adding ZK proofs
  - Enforce authenticity even if participants compromised
  - Preserve secrecy if everybody is honest
- Automatic verification of the generated protocols
  - We use type system for ZK [Backes, Hritcu & Maffei, CCS '08]
    - now extended to handle security despite compromise
- Automatic code generation
  - Spi2RCF: from Spi calculus to ML fragment

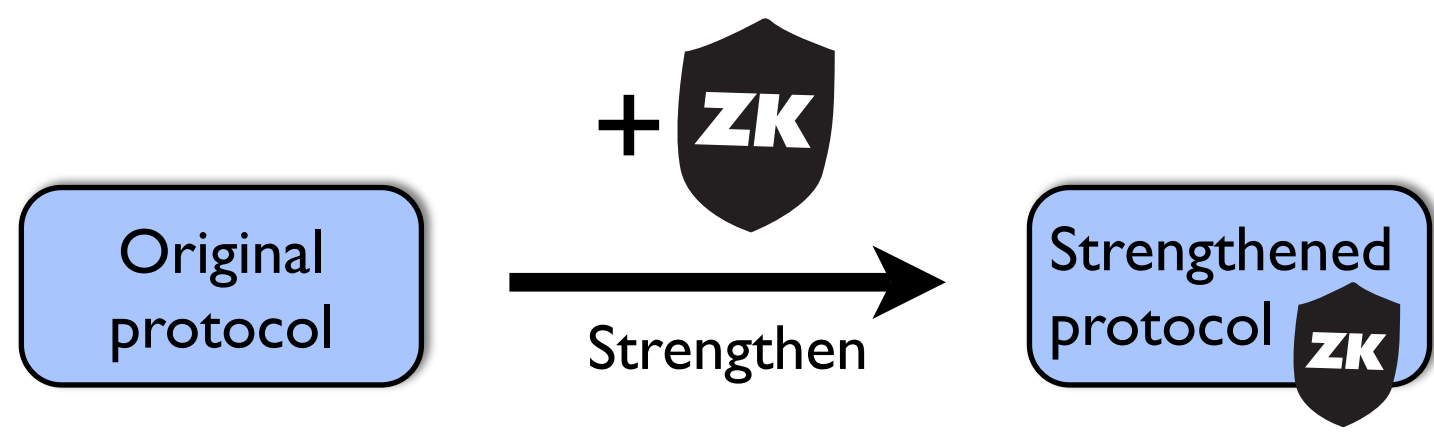




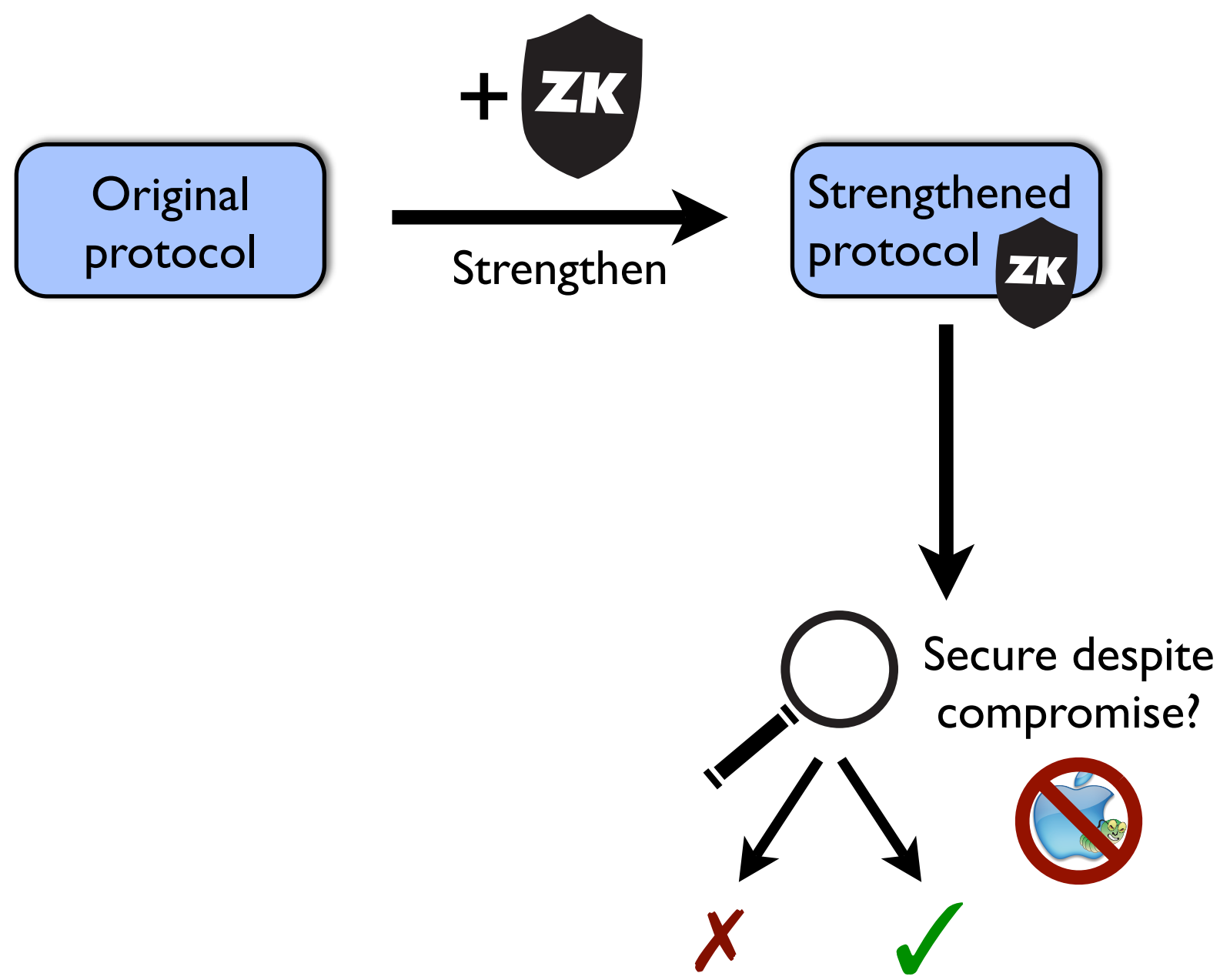
# The big picture

Original  
protocol

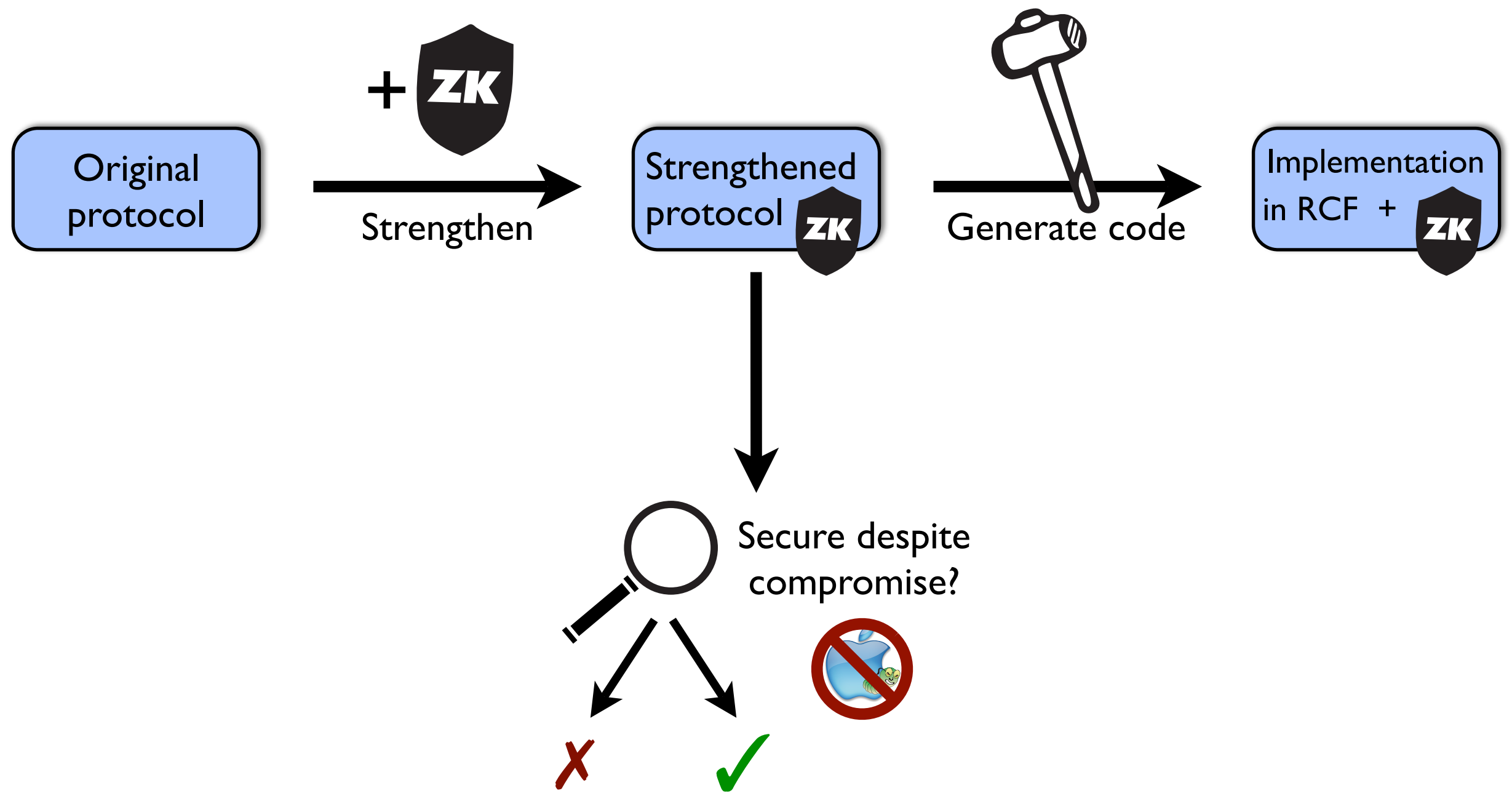
# The big picture



# The big picture



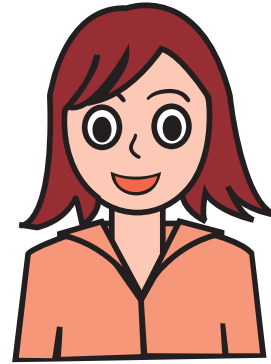
# The big picture



# A simple protocol



proxy



user

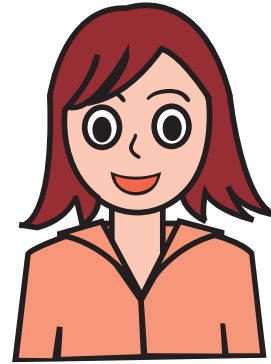


store

# A simple protocol



proxy



user



store

$(u, q, p_{wd})$

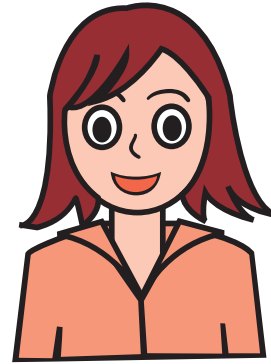




# A simple protocol



proxy



user



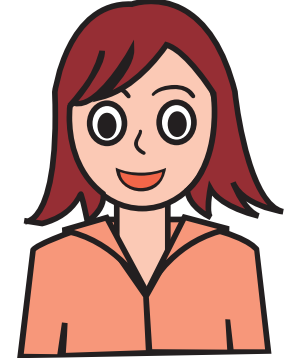
store

$\leftarrow \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

# A simple protocol



proxy



user



store

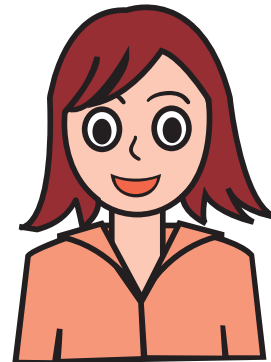
$\leftarrow \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

$\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-) \rightarrow$

# A simple protocol



proxy



user



store

$\leftarrow \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

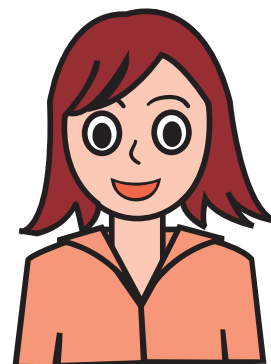
$\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-) \rightarrow$

- This protocol is secure if all participants are honest ( $p_{wd}$  is secret and  $q$  is authentic)

# A simple protocol



proxy



user



store

$\text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

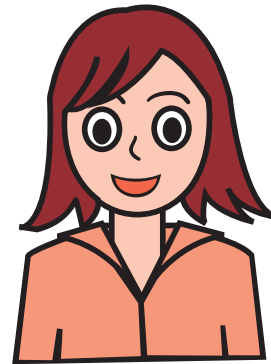
$\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-)$

- This protocol is secure if all participants are honest ( $p_{wd}$  is secret and  $q$  is authentic)
- ... but insecure if the proxy is compromised

# A simple protocol



proxy



user



store

$\text{sign}(\text{enc}((u, q, p_{\text{wd}}), k_{\text{PE}}^+), k_{\text{U}}^-)$

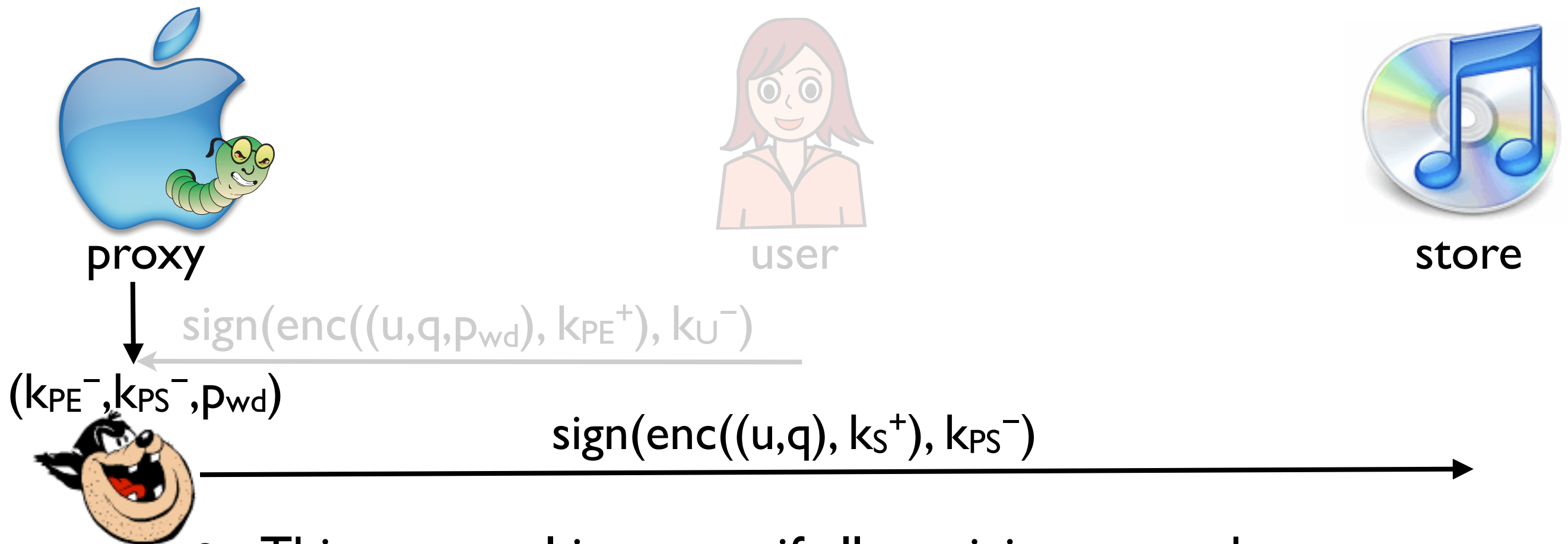
$(k_{\text{PE}}^-, k_{\text{PS}}^-, p_{\text{wd}})$

$\text{sign}(\text{enc}((u, q), k_{\text{S}}^+), k_{\text{PS}}^-)$



- This protocol is secure if all participants are honest ( $p_{\text{wd}}$  is secret and  $q$  is authentic)
- ... but insecure if the proxy is compromised
- compromised proxy can leak  $p_{\text{wd}}$  (unavoidable)

# A simple protocol



- This protocol is secure if all participants are honest ( $p_{\text{wd}}$  is secret and  $q$  is authentic)
- ... but insecure if the proxy is compromised
  - compromised proxy can leak  $p_{\text{wd}}$  (unavoidable)
  - **compromised proxy can fake request from the user (break authenticity)**





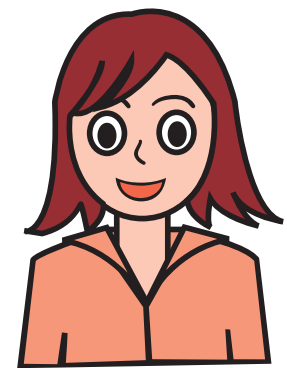
# Transformation



# Trying to strengthen the protocol



proxy



user



store

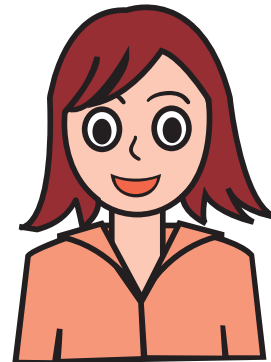
$\leftarrow \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

$\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-) \rightarrow$

# Trying to strengthen the protocol



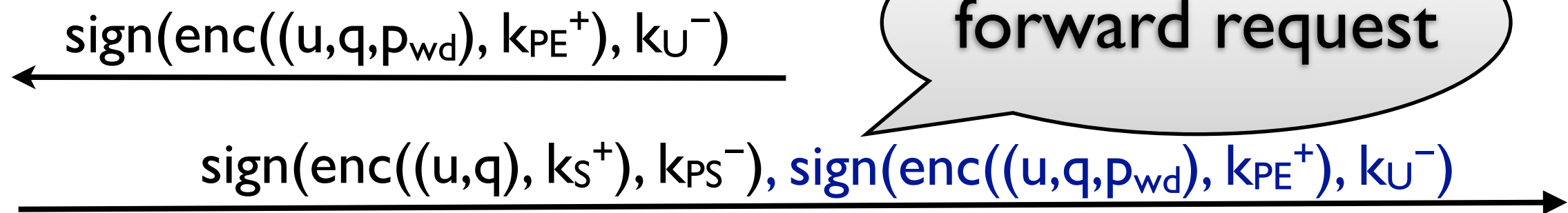
proxy



user



store

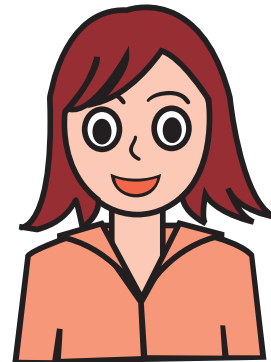


- Store can check user's signature on “ $\text{enc}((q, p_{wd}), k_{PE}^+)$ ”

# Trying to strengthen the protocol



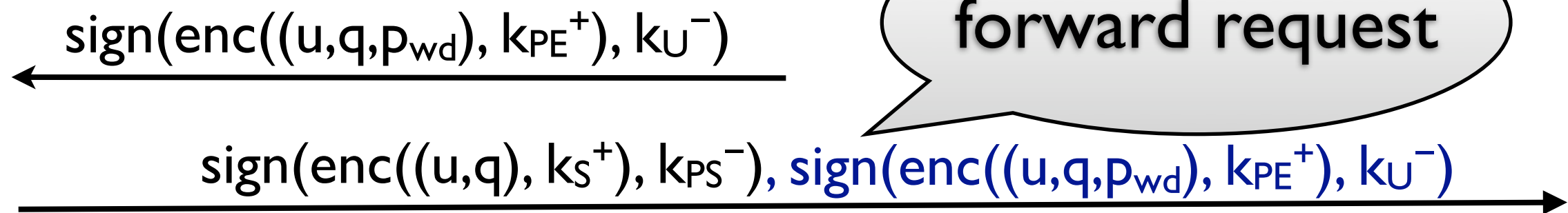
proxy



user



store

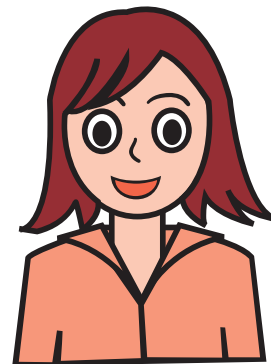


- Store **can check** user's signature on " $\text{enc}((q, p_{wd}), k_{PE}^+)$ "
- Store **cannot decrypt** " $\text{enc}((u, q, p_{wd}), k_{PE}^+)$ " in order to check  $q$

# Trying to strengthen the protocol



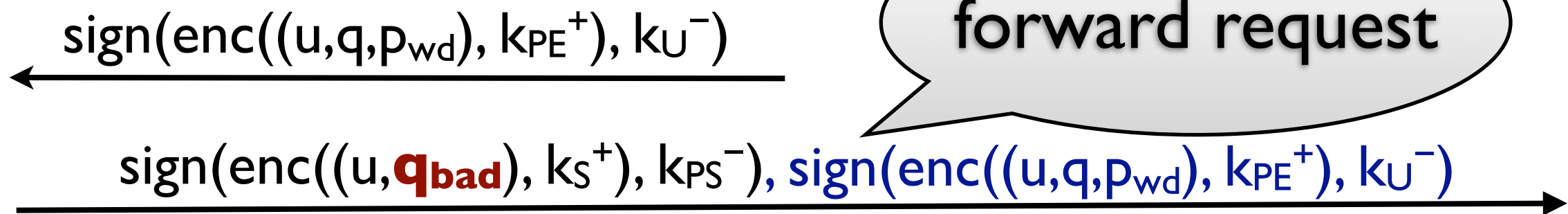
proxy



user



store

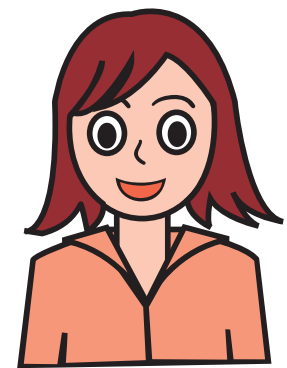


- Store can check user's signature on "enc((q, p<sub>wd</sub>), k<sub>PE</sub><sup>+</sup>)"
- Store cannot decrypt "enc((u, q, p<sub>wd</sub>), k<sub>PE</sub><sup>+</sup>)" in order to check q
- ... still insecure if proxy comprised (message substitution attack)

# Using non-interactive ZK



proxy



user



store

$\leftarrow \text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_U^-)$

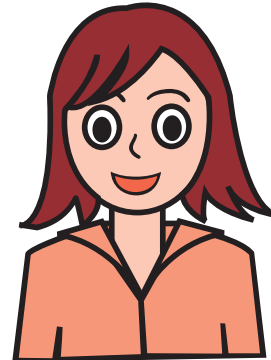
$\xrightarrow{\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)}$



# Using non-interactive ZK



proxy



user



store

$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_U^-)$



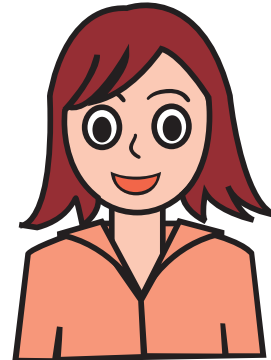
$\text{zk}_S(k_{PE}^-, q, p_{wd}; \text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-), u)$



# Using non-interactive ZK



proxy



user



store

$$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_U^-)$$


$$\text{zk}_S(k_{PE}^-, q, p_{wd}; \text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-), u)$$

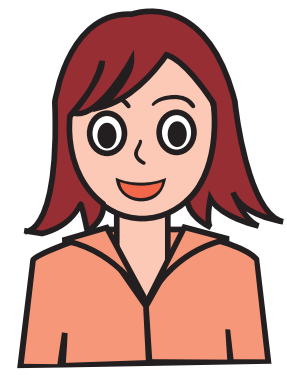

secret  
witnesses

[Backes, Maffei & Unruh, S&P '08]

# Using non-interactive ZK



proxy



user



store

$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_U^-)$



$zk_S(k_{PE}^-, q, p_{wd}; \text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-), u)$



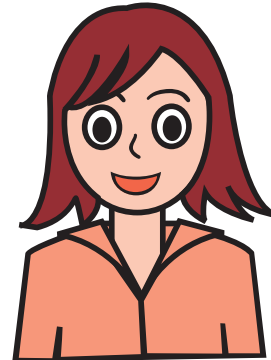
public terms

[Backes, Maffei & Unruh, S&P '08]

# Using non-interactive ZK



proxy



user



store

$$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_{U}^-)$$

$$\text{zk}_S(k_{PE}^-, q, p_{wd}; \text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_{U}^-), u)$$

statement (= Boolean formula over equalities between terms with placeholders)

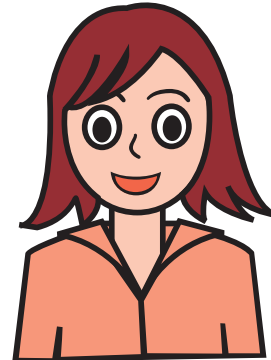
$$S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (\beta_3, \alpha_2, \alpha_3)$$

[Backes, Maffei & Unruh, S&P '08]

# Using non-interactive ZK



proxy



user



store

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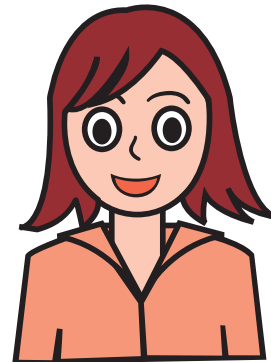

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# Using non-interactive ZK



proxy



user



store

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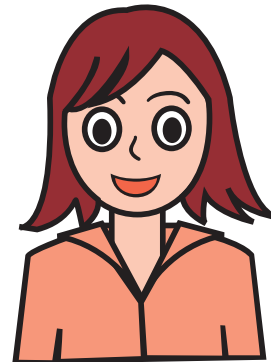

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# Using non-interactive ZK



proxy



user



store

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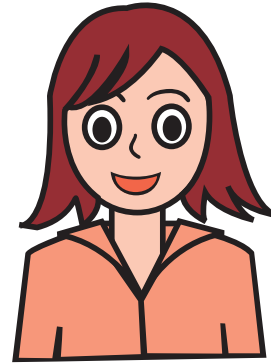

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# Using non-interactive ZK



proxy



user



store

$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_U^-)$



$\text{zk}_S(k_{PE}^-, q, p_{wd}; \text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-), u)$



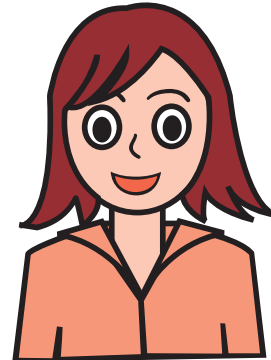
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# Using non-interactive ZK



proxy



user



store

$$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_U^-)$$

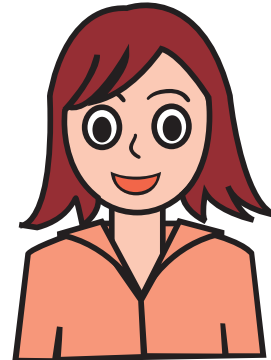

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# Using non-interactive ZK



proxy



user



store

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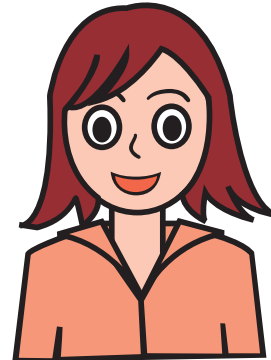

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user



store

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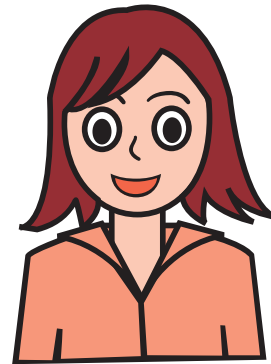

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- The proxy has to prove that its message is correctly generated from a request he received from the user

# Using non-interactive ZK



proxy



user



store

$$\text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_{U}^-)$$

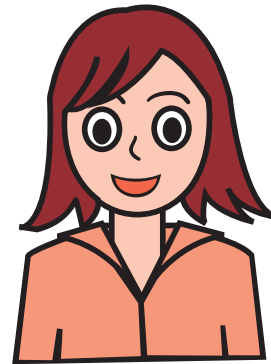

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- The proxy has to prove that its message is correctly generated from a request he received from the user
- Compromised proxy can no longer cheat

# Using non-interactive ZK



proxy



user



store

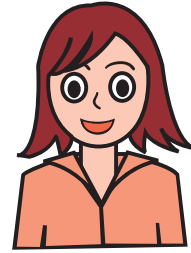
$$\leftarrow \text{sign}(\text{enc}((q, p_{wd}), k_{PE}^+), k_{U}^-)$$

$$\text{zk}_S(k_{PE}^-, q, p_{wd}; \text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-), \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_{U}^-), u)$$

- The proxy has to prove that its message is correctly generated from a request he received from the user
- Compromised proxy can no longer cheat
- No secret data is revealed if everybody is honest



proxy



user

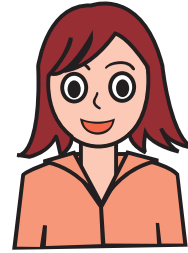


store

$\leftarrow \text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$



proxy



user



store

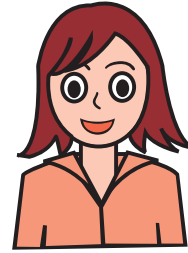
←  $\text{sign}(\text{enc}((u, q, p_{\text{wd}}), k_{\text{PE}}^+), k_{\text{U}}^-)$

```
let user = new q;  
      out(c1,  $\text{sign}(\text{enc}((u, q, p_{\text{wd}}), k_{\text{PE}}^+), k_{\text{U}}^-)$ ).
```

```
let proxy =  
  in(c1, x);  
  let (=u, xq, =pwd) =  $\text{dec}(\text{check}(x, k_{\text{U}}^+), k_{\text{PE}}^-)$  in  
  ...
```



proxy



user



store

←  $\text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

$\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-)$  →

```
let user = new q;  
      out(c1,  $\text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$ ).
```

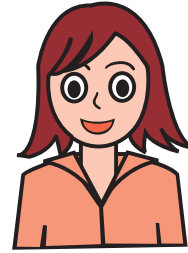
```
let proxy =  
  in(c1, x);  
  let (=u, xq, =pwd) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  in  
  out(c2,  $\text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-)$ ).
```

```
let store = in(c2, z);  
  let (xu, xq) =  $\text{dec}(\text{check}(z, k_{PS}^+), k_S^-)$  in  
  ...
```





proxy



user



store

←  $\text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$

$\text{sign}(\text{enc}((u, q), k_S^+), k_{PS}^-)$  →

```
let user = new q;  
      out(c1,  $\text{sign}(\text{enc}((u, q, p_{wd}), k_{PE}^+), k_U^-)$ ).
```

```
let proxy =  
  in(c1, x);  
  let (=u, xq, =pwd) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  in  
  out(c2,  $\text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-)$ ).
```

```
let store = in(c2, z);  
  let (xu, xq) =  $\text{dec}(\text{check}(z, k_{PS}^+), k_S^-)$  in  
  ...
```

```
new kU-, kPE-, kPS-, kS-, pwd; (user | proxy | store )
```

# Transforming Processes

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}$ ; (user | proxy' | store )

# Transforming Processes

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );


**let** ( $=u, x_q, =p_{wd}$ ) = dec(check( $x, k_U^+$ ),  $k_{PE}^-$ ) **in**

**out**( $c_2, z_{k_S}(\quad, \quad, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, \quad)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd};$  (user | proxy' | store )

# Transforming Processes



automatically  
generate zk  
statement

**stmt**  $S = \text{true}$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_s}(\quad, \quad, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, \quad)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

automatically  
generate zk  
statement

**stmt**  $S = \text{true}$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, \quad, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, \quad)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

prove that  
message is correctly  
generated

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((u, x_q), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let**  $(=u, x_q, =p_{wd}) = \text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, \quad, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, \quad)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

Secrecy analysis

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((u, x_q), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, \quad, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, \quad)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((u, x_q), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, \quad, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$



# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, x_q), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, \quad, \quad; \underline{\text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-)}, \quad, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, x_q), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, x_q, \quad; \underline{\text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-)}, \quad, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, x_q, \quad; \underline{\text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-)}, \quad, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, \underline{x_q}, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, u)$ ).

**let** store = ...

term that depends on  
previous input

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ )  
**let** ( $=u, x_q = p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**  
**out**( $c_2, z_{k_S}(\quad, \underline{x_q}, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, u)$ ).

**let** store = ...

term that depends on  
previous input

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

We represent precise dependency symbolically

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(x, k_U^+), k_{PE}^-) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ )  
**let** ( $=u, x_q, p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**  
**out**( $c_2, z_{k_S}(\quad, \underline{x_q}, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), \quad, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(x, k_U^+), k_{PE}^-) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, x_q, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

forward previous input

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), k_{PE}^-) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(\quad, x_q, \quad; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$



# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), k_{PE}^-) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let**  $(=u, x_q, =p_{wd}) = \text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(k_{PE}^-, x_q, \quad ; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

Asymmetry caused by  $k_s^-$   
being unknown to the proxy

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_s^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_s^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), k_{PE}^-) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let**  $(=u, x_q, =p_{wd}) = \text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_s}(k_{PE}^-, x_q, \quad ; \text{sign}(\text{enc}((u, x_q), k_s^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_s^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let**  $(=u, x_q, =p_{wd}) = \text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(k_{PE}^-, x_q, \text{ ; sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

*public terms:*  $c_1, c_2, u, x, k_{PS}^+, k_S^+, k_U^+$

*secret terms:*  $x_q, p_{wd}, k_{PE}^-, k_{PS}^-$

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (u, x_q, p_{wd})$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(k_{PE}^-, x_q, p_{wd}; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

Shows that outputs correctly  
constructed from inputs

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (\beta_3, \alpha_2, \alpha_3)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let** ( $=u, x_q, =p_{wd}$ ) =  $\text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z_{k_S}(k_{PE}^-, x_q, p_{wd}; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store = ...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store})$

# Transforming Processes

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (\beta_3, \alpha_2, \alpha_3)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let**  $(=u, x_q, =p_{wd}) = \text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z k_S(k_{PE}^-, x_q, p_{wd}; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store' = **in**( $c_2, z$ );

**let**  $(x_u, x_q) = \text{dec}(\text{check}(z, k_{PS}^+), k_S^-)$  **in**

...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store}')$

# Transforming Processes

**stmt**  $S = \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (\beta_3, \alpha_2, \alpha_3)$

**let** user = ...

**let** proxy' =

**in**( $c_1, x$ );

**let**  $(=u, x_q, =p_{wd}) = \text{dec}(\text{check}(x, k_U^+), k_{PE}^-)$  **in**

**out**( $c_2, z k_S(k_{PE}^-, x_q, p_{wd}; \text{sign}(\text{enc}((u, x_q), k_S^+), k_{PS}^-), x, u)$ ).

**let** store' = **in**( $c_2, z$ );

**let**  $(\beta_1, \beta_2, \beta_3) = \text{ver}_S(z)$  **in**

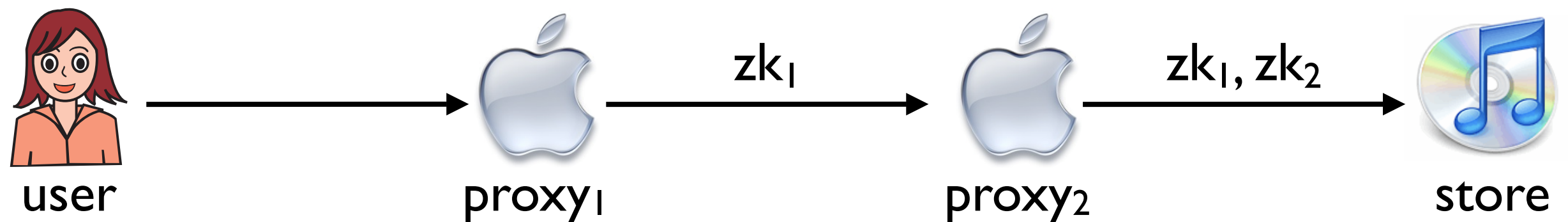
**let**  $(x_u, x_q) = \text{dec}(\text{check}(\beta_1, k_{PS}^+), k_S^-)$  **in**

...

**new**  $k_U^-, k_{PE}^-, k_{PS}^-, k_S^-, p_{wd}; (\text{user} \mid \text{proxy}' \mid \text{store}')$

# Further complications

- Forwarding zero-knowledge proofs
  - Ensure correct behavior of all protocol participants



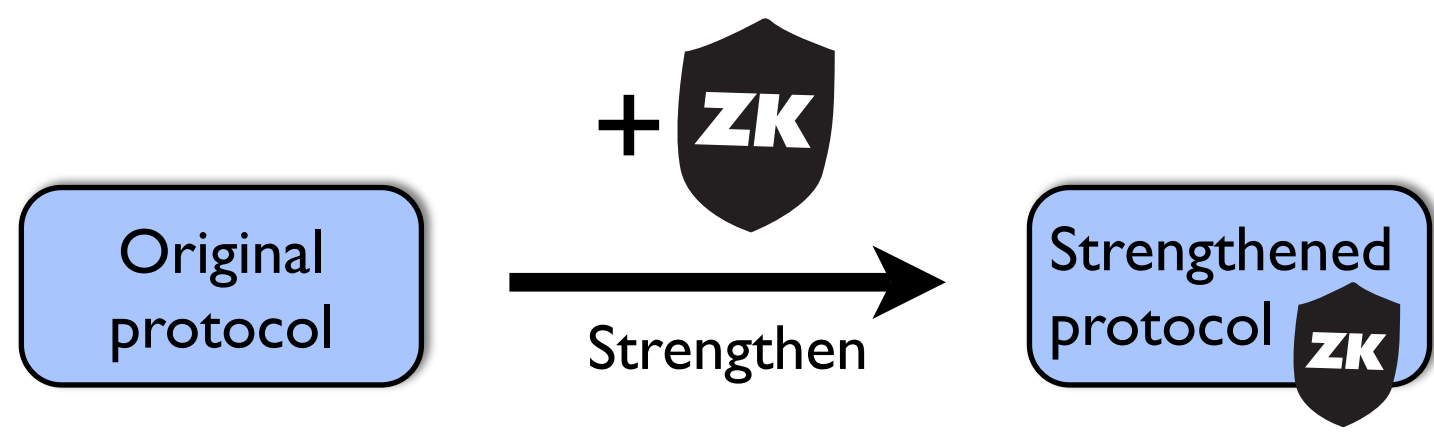
- Symmetric encryption: add proof of identity
  - digital signature or ZK proof (can preserve some anonymity)
- Transforming types



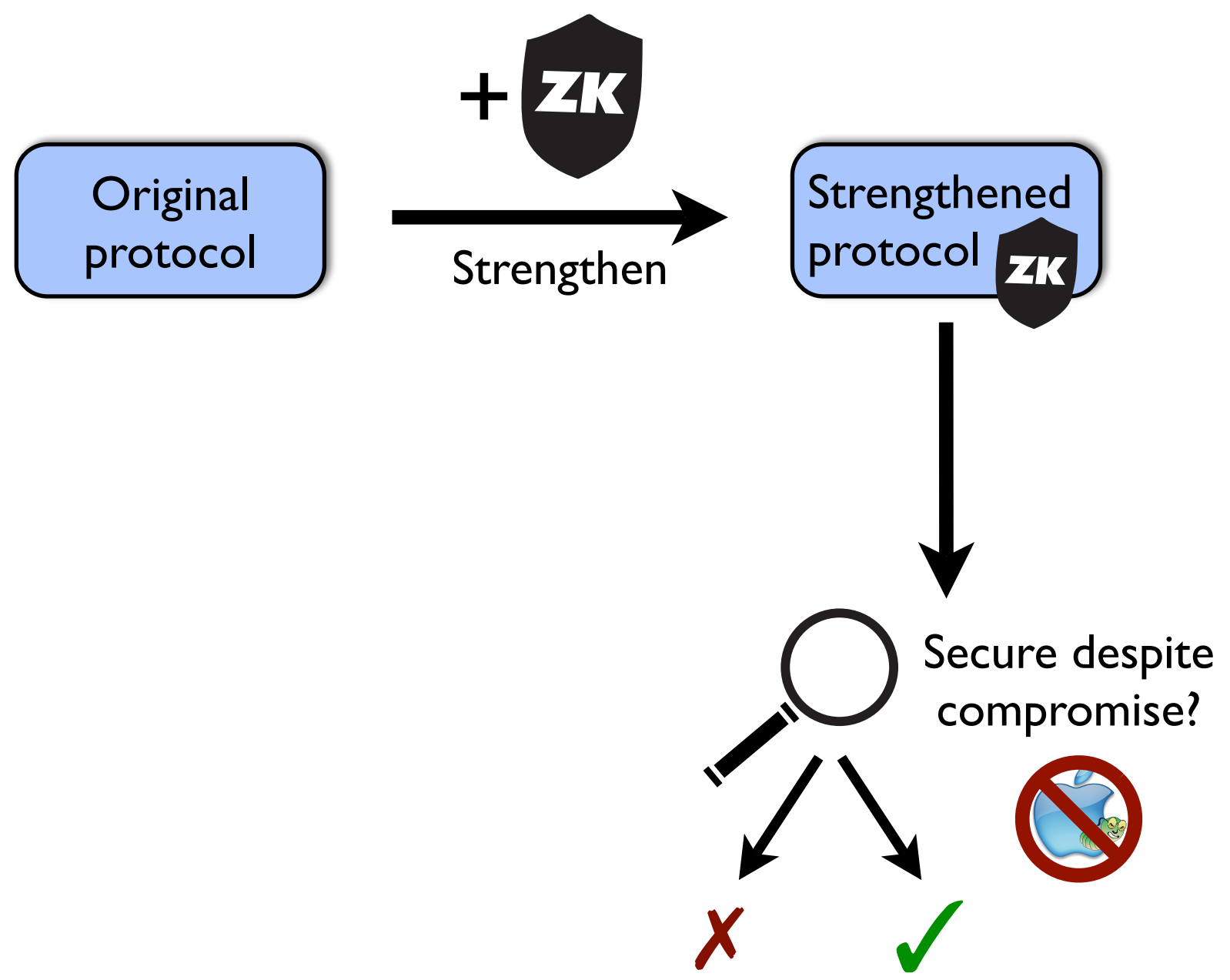
# Type System



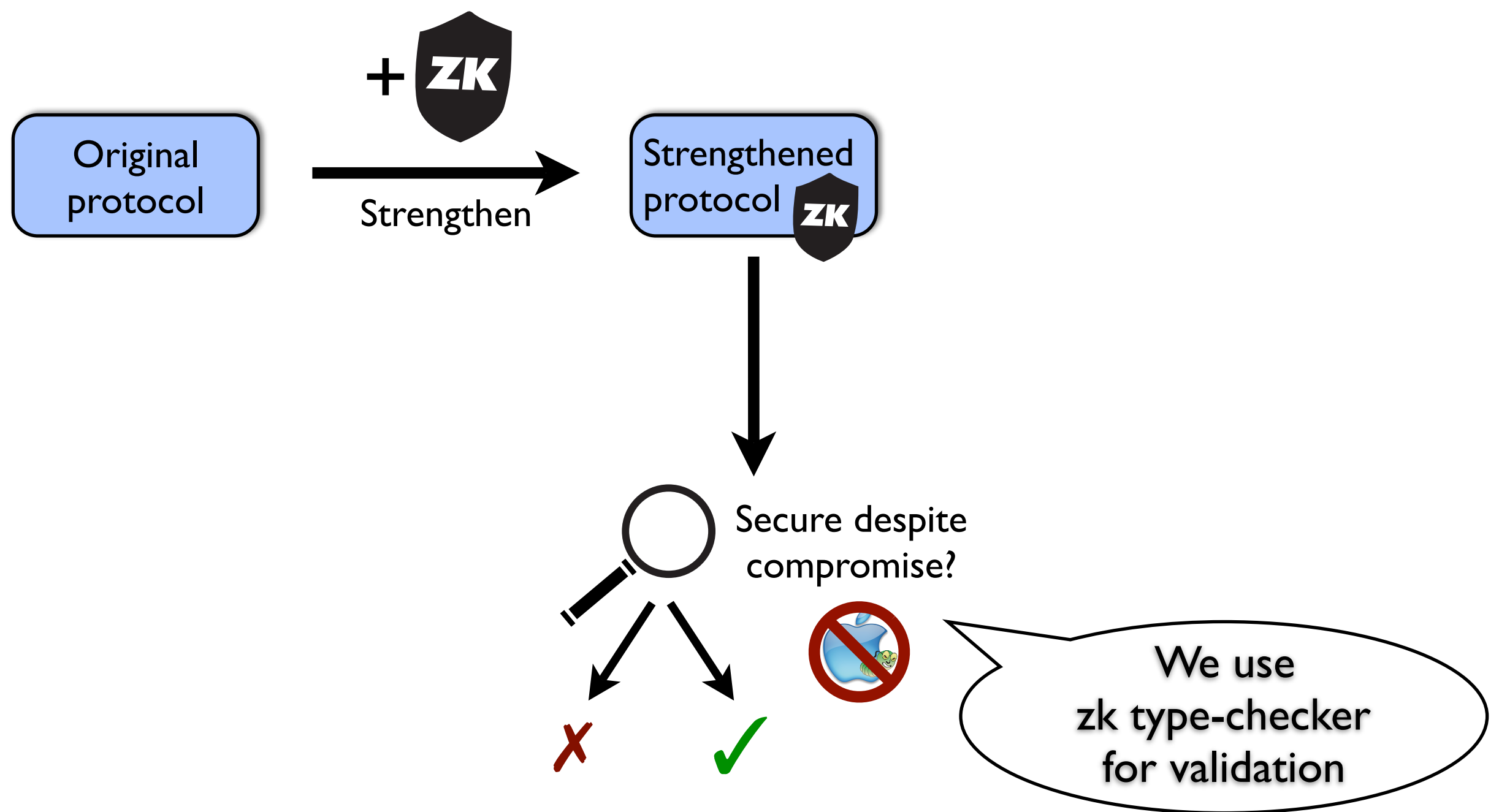
# Translation validation



# Translation validation

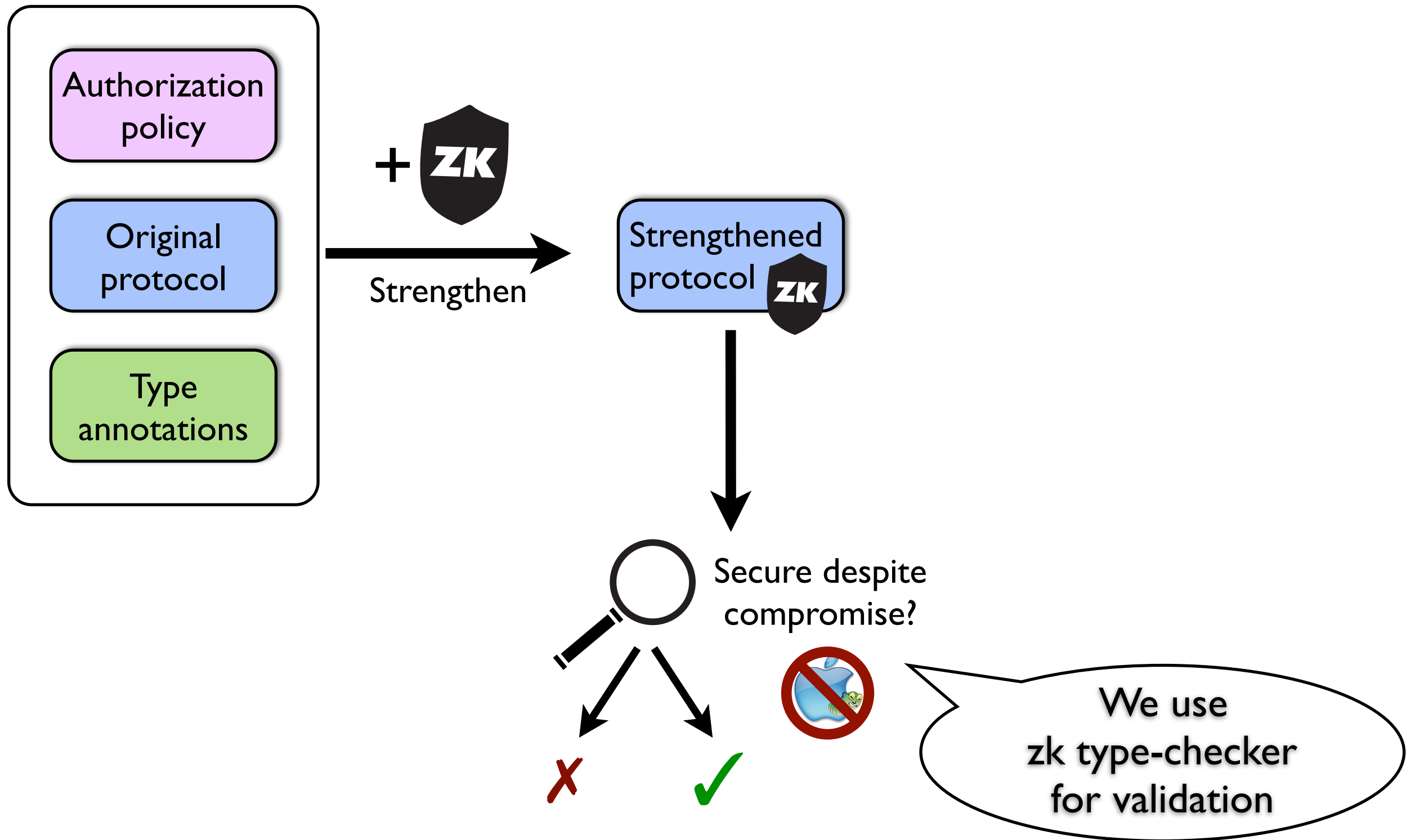


# Translation validation



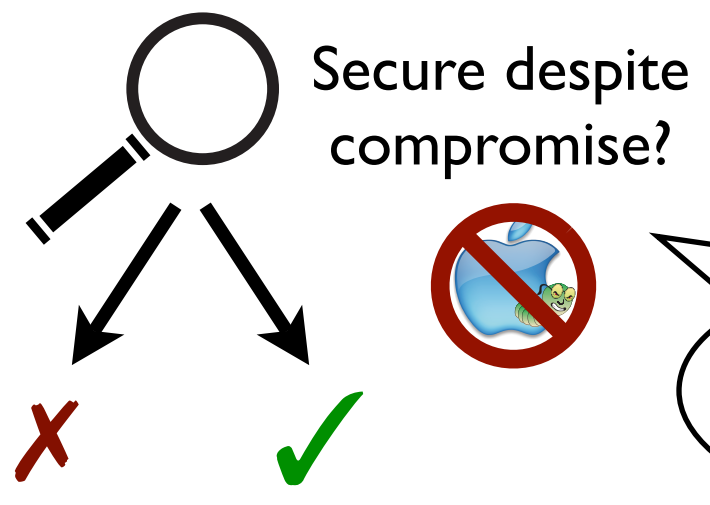
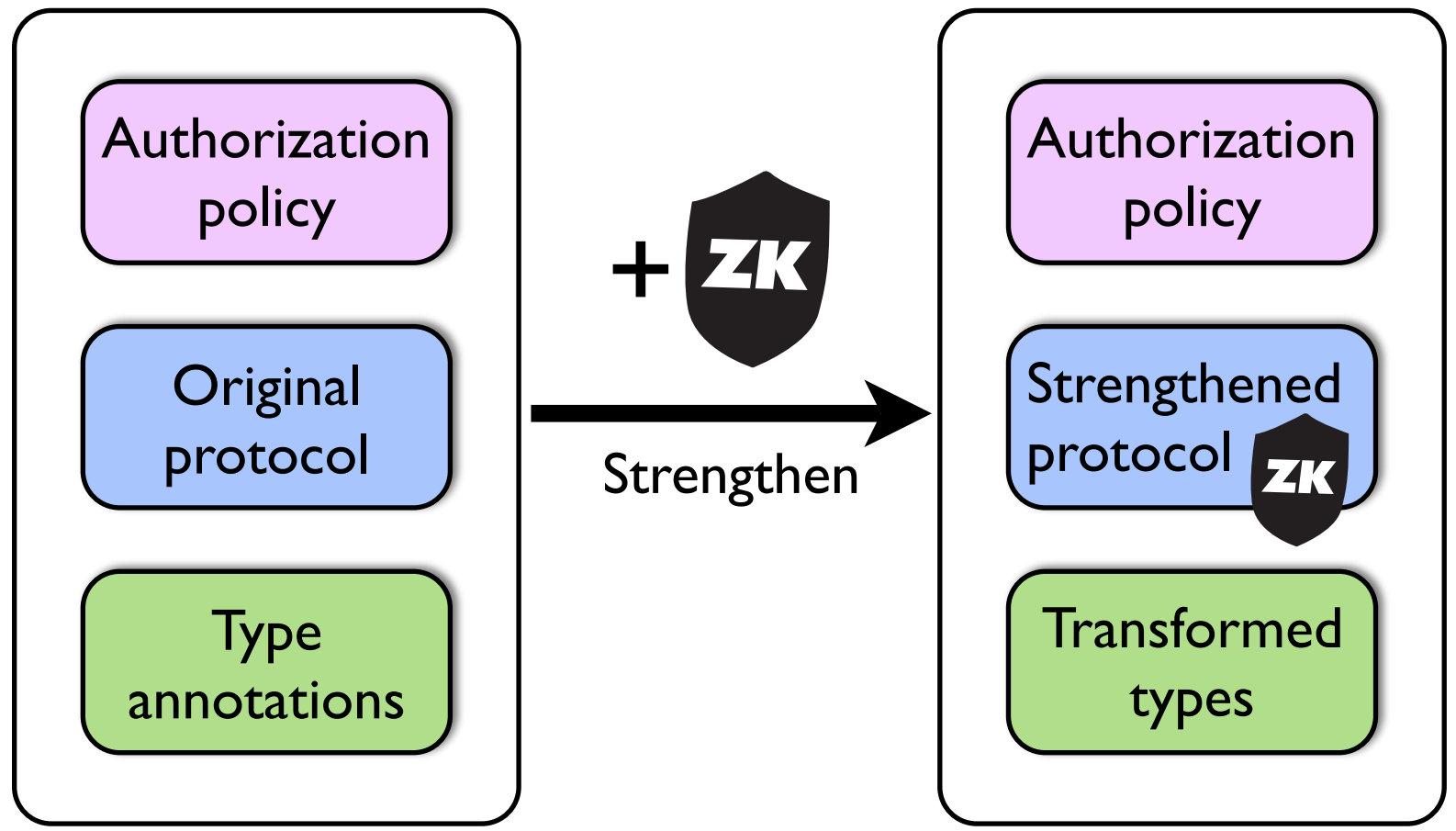
[Backes, Hrițcu & Maffei, CCS '08]  
now with  $\wedge$  +  $\vee$  + logical kinding

# Translation validation



[Backes, Hrițcu & Maffei, CCS '08]  
now with  $\wedge$  +  $\vee$  + logical kinding

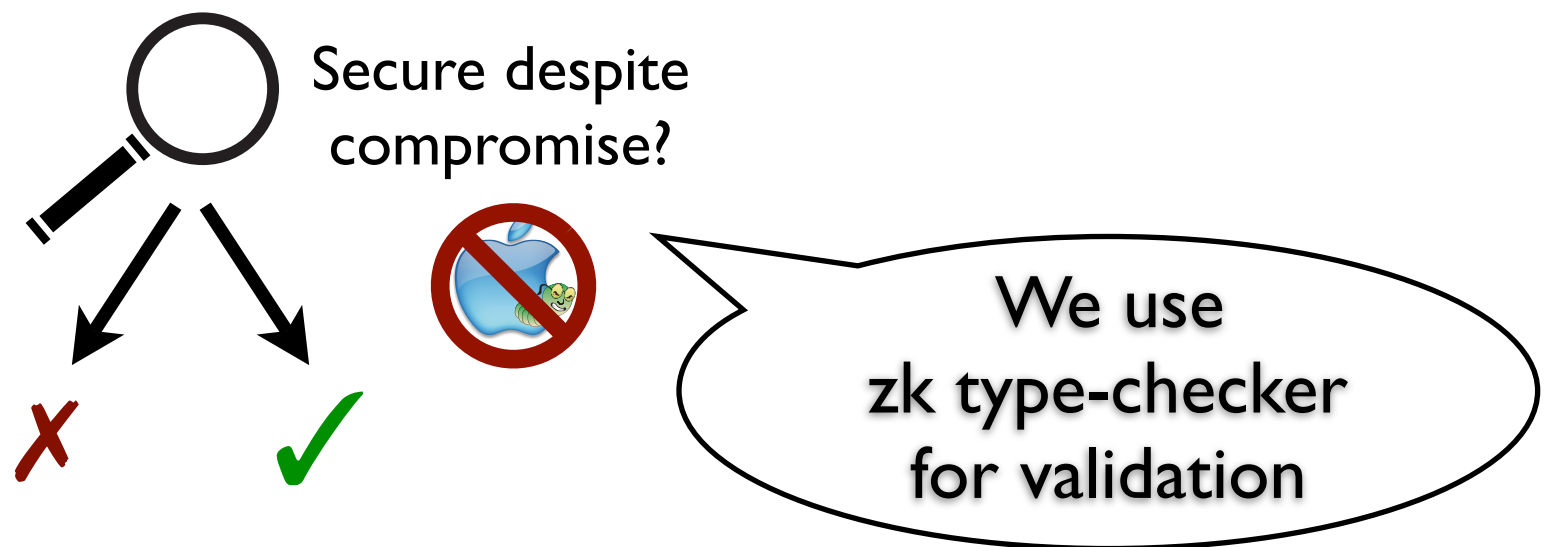
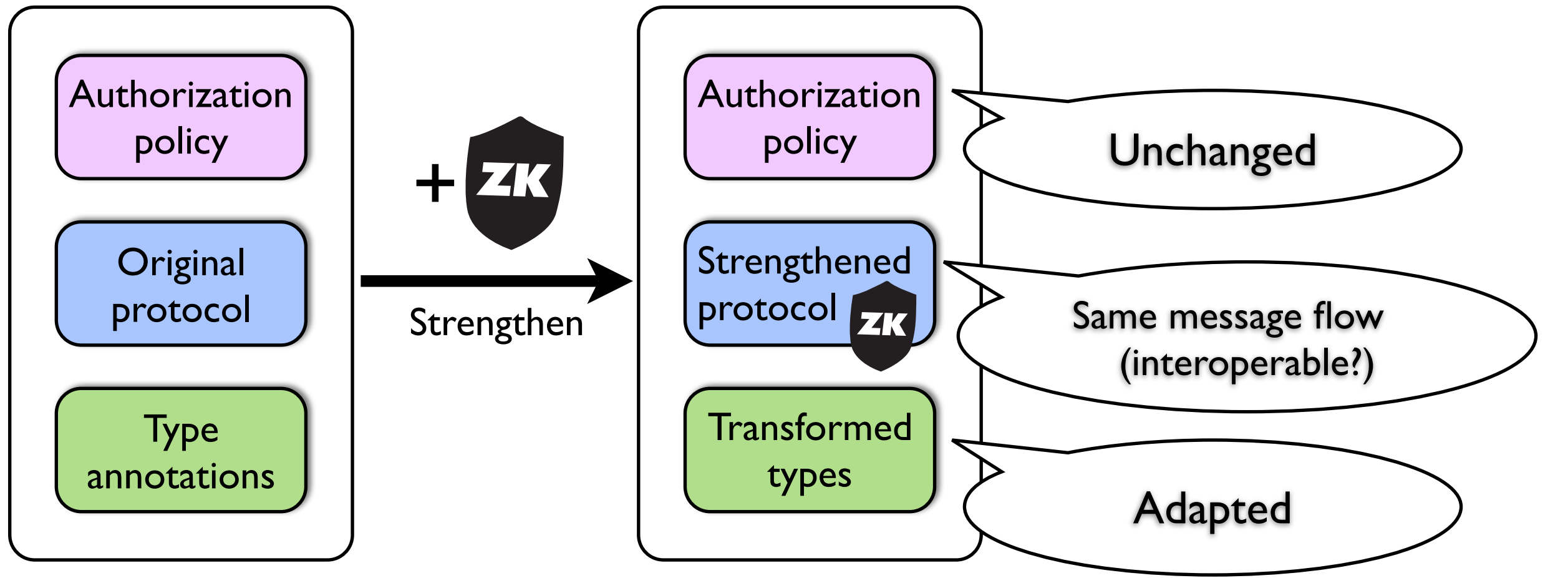
# Translation validation



We use zk type-checker for validation

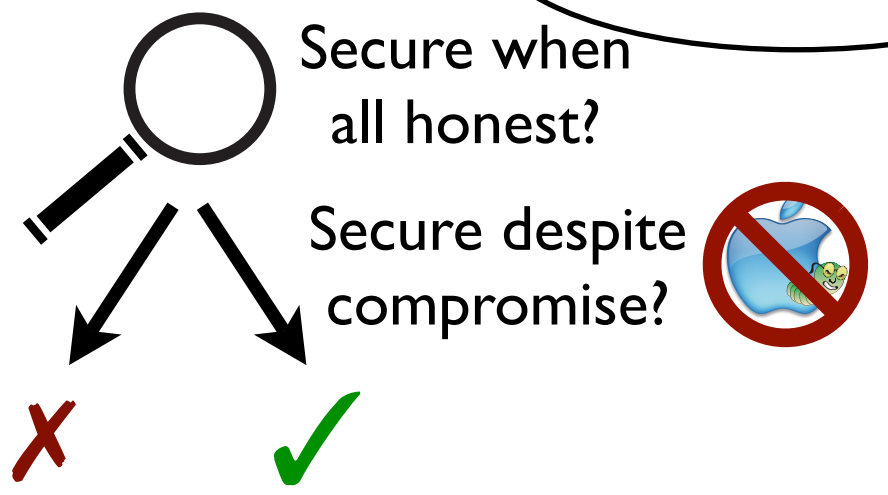
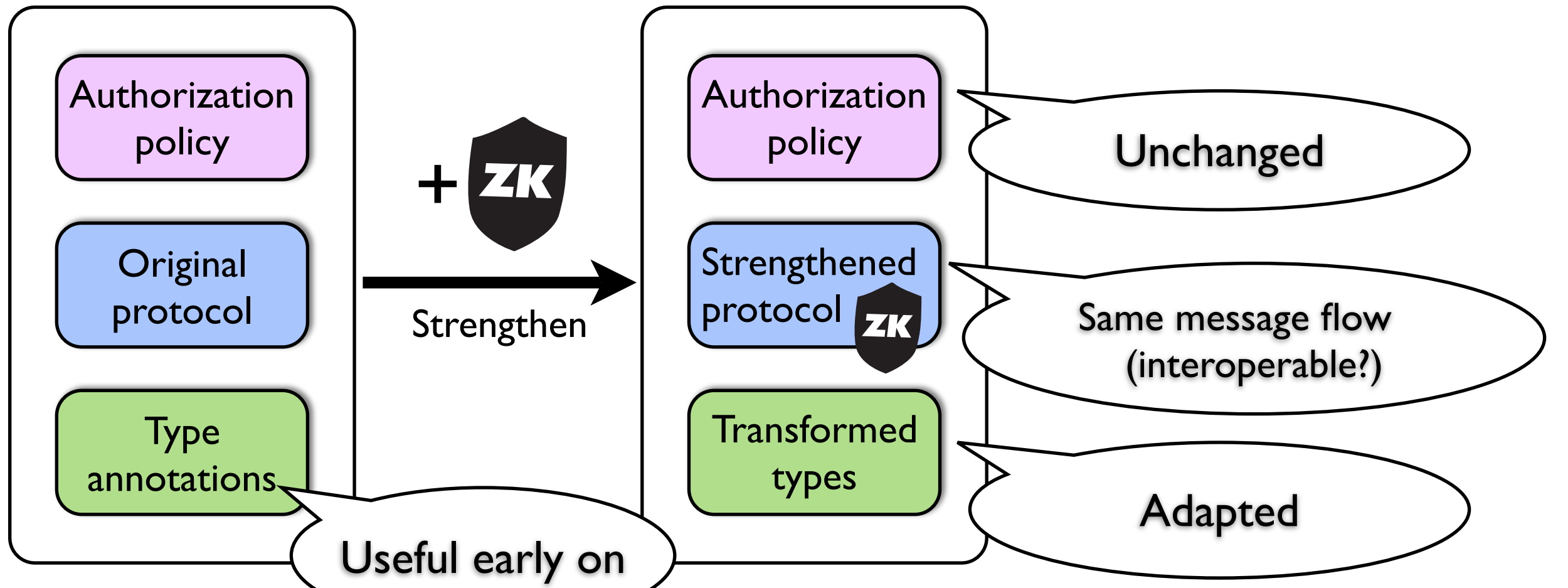
[Backes, Hrițcu & Maffei, CCS '08]  
now with  $\wedge$  +  $\vee$  + logical kinding

# Translation validation

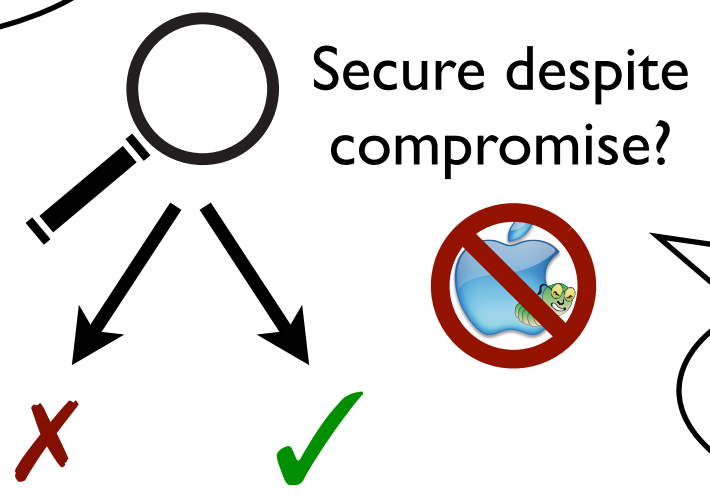


[Backes, Hrițcu & Maffei, CCS '08]  
 now with  $\wedge + \vee +$  logical kinding

# Translation validation



[Fournet, Gordon & Maffei, CSF '07]



[Backes, Hrițcu & Maffei, CCS '08]  
now with  $\wedge + \vee +$  logical kinding

We use zk type-checker for validation



# Type system

- Enhancement of [Backes, Hritcu & Maffei, CCS '08] which extends [Fournet, Gordon & Maffei, CSF '07]

# Type system

- Enhancement of [Backes, Hritcu & Maffei, CCS '08] which extends [Fournet, Gordon & Maffei, CSF '07]
- Example types

# Type system

- Enhancement of [Backes, Hritcu & Maffei, CCS '08] which extends [Fournet, Gordon & Maffei, CSF '07]
- Example types
  - `u: Un`



Public message - can be sent to the attacker

# Type system

- Enhancement of [Backes, Hritcu & Maffei, CCS '08] which extends [Fournet, Gordon & Maffei, CSF '07]
- Example types
  - $u$ : Un
  - $p_{wd}$ : Private



Secret and authentic  
- not known to the  
attacker

# Type system

- Enhancement of [Backes, Hritcu & Maffei, CCS '08] which extends [Fournet, Gordon & Maffei, CSF '07]
- Example types
  - $u: Un$
  - $p_{wd}: \text{Private}$
  - $T_2 = (x_u : Un, \{x_q : Un \mid \text{Request}(x_u, x_q) \wedge \text{Registered}(x_u)\})$   
 $(u, q): T_2$

Refinement type -  
conveys logical formula

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  - $k_{PS}^-: SigKey(PubEnc(T_2))$

Key only used to sign  
encryptions of terms of type  $T_2$   
(if proxy is honest)

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  - $z: ZKProof_S(y:T, \exists x.C)$



Zero-knowledge proof  
of statement  $S$

# Enhancements

- Added union and intersection types



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- Conditionally secure types (depending on compromise scenario)  
 $\text{PrivateUnlessP} = \{\text{Private} \mid \neg \text{Compromised}(p)\} \vee \{\text{Un} \mid \text{Compromised}(p)\}$   
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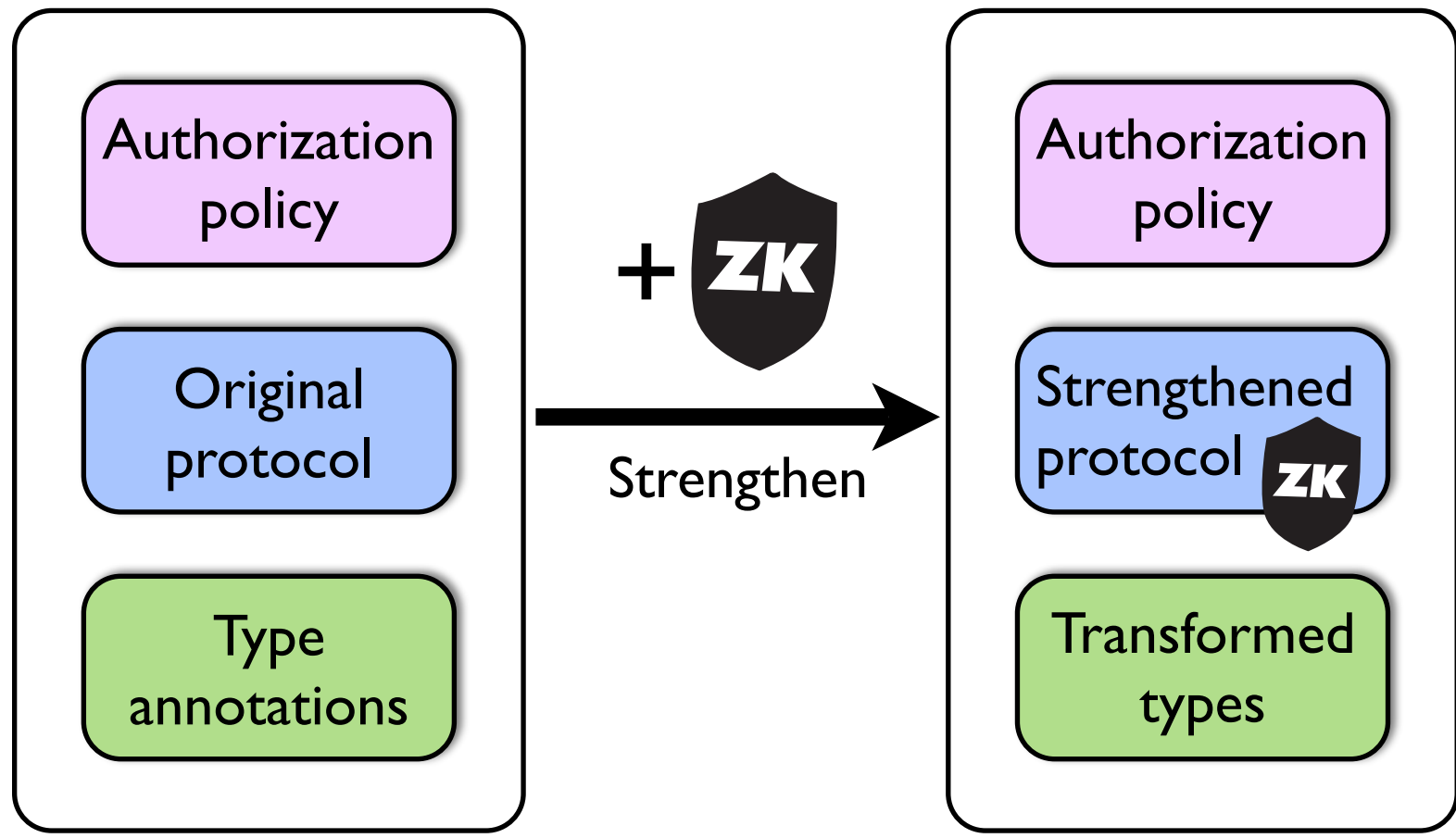
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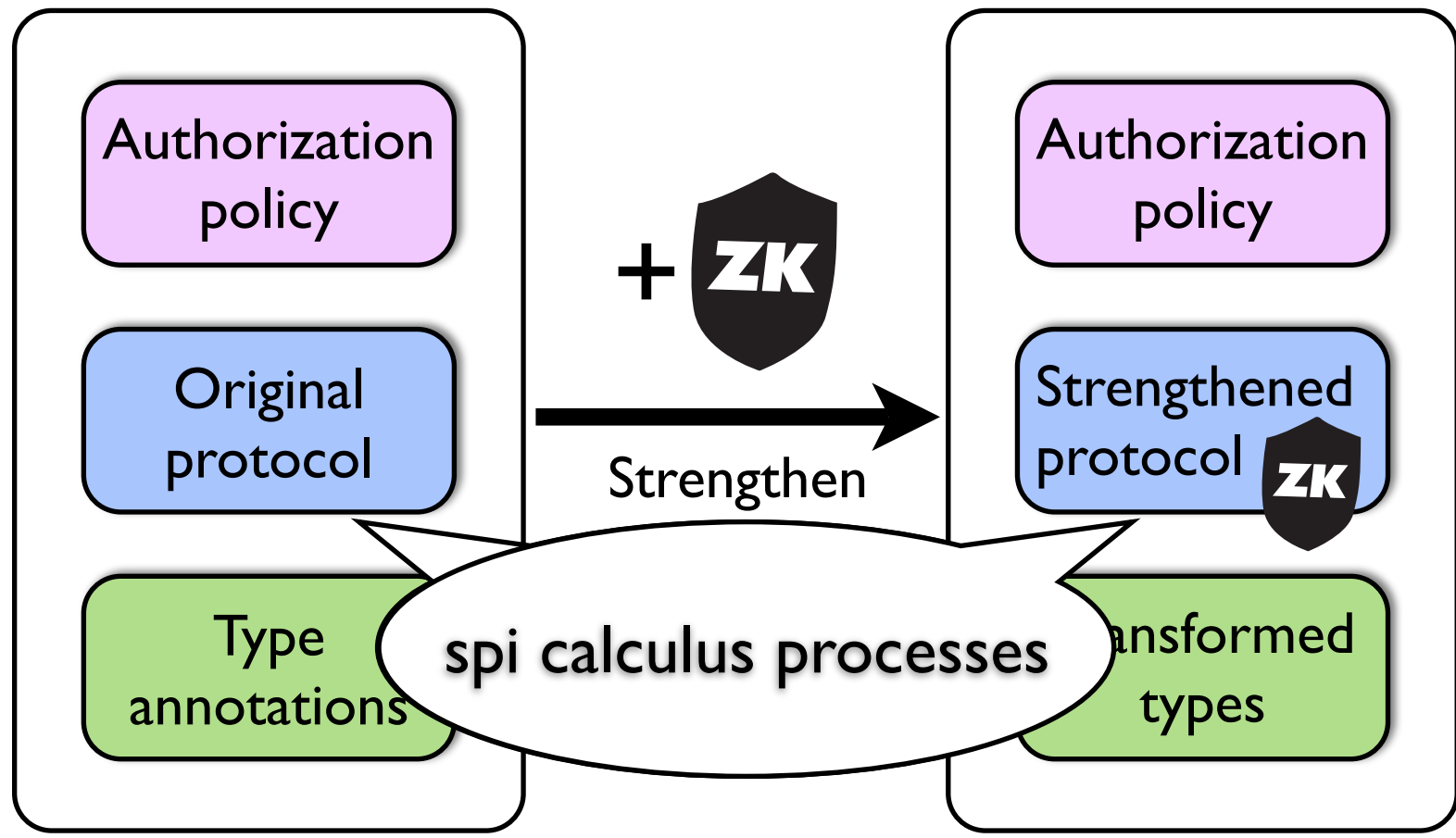
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# Automatic code generation

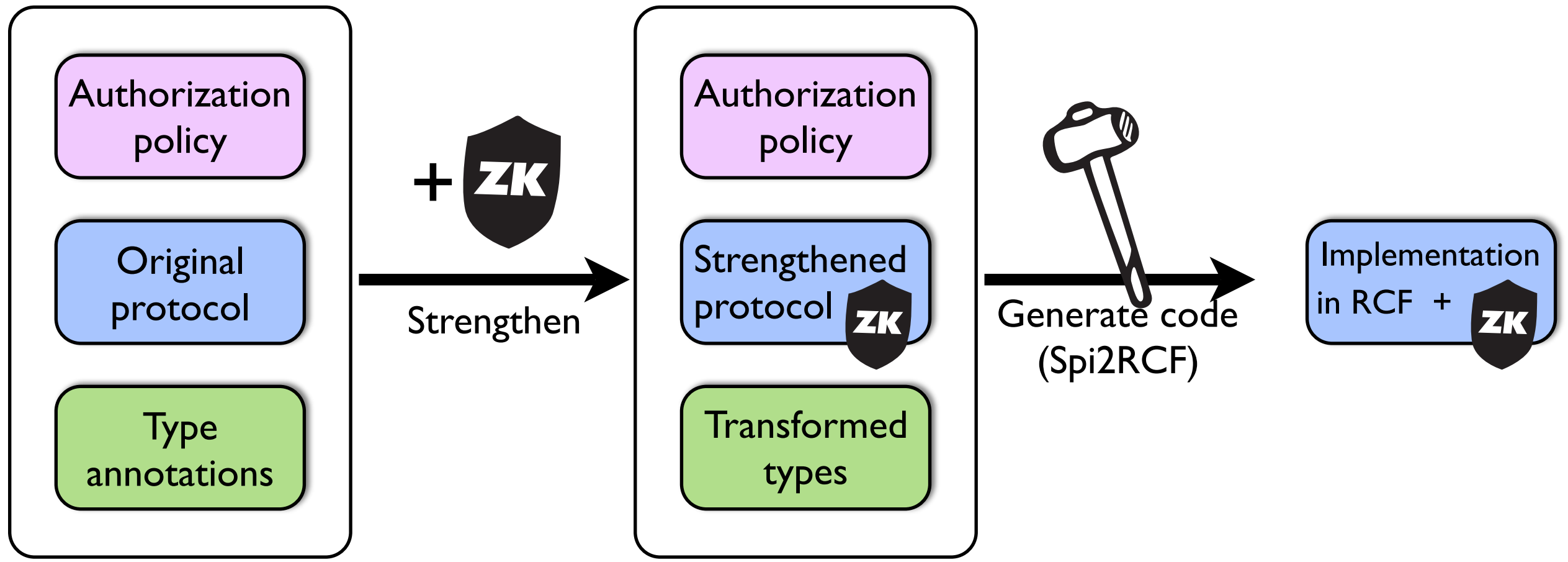




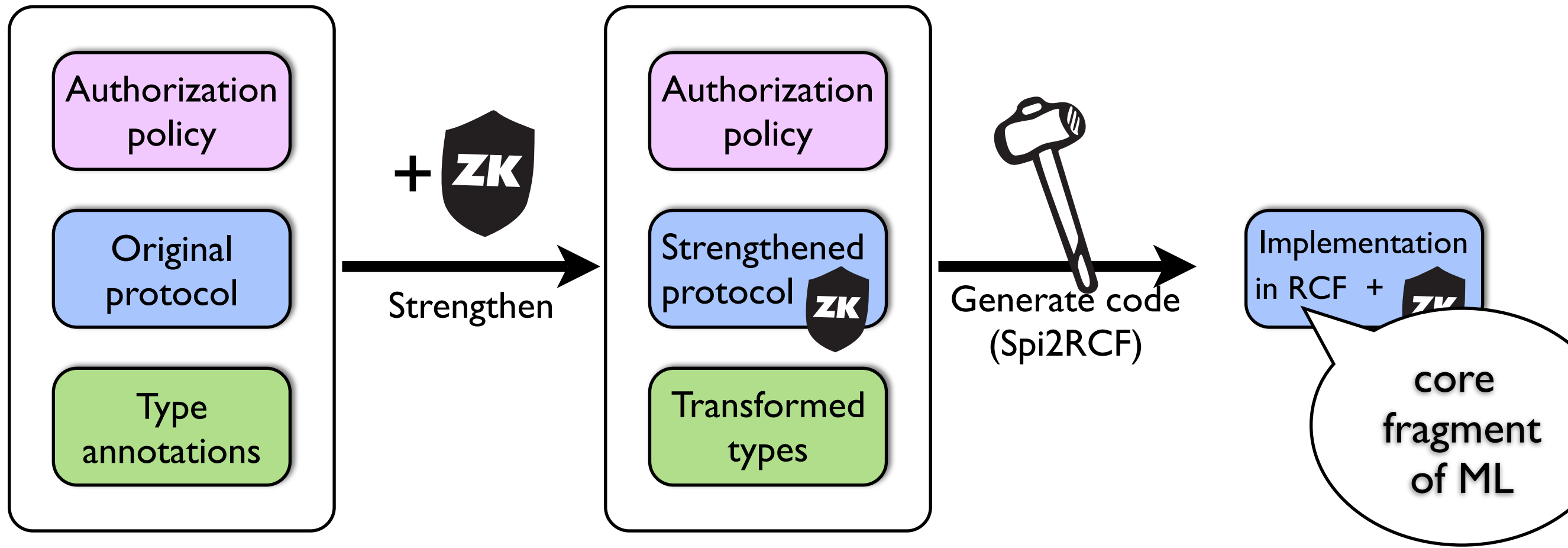
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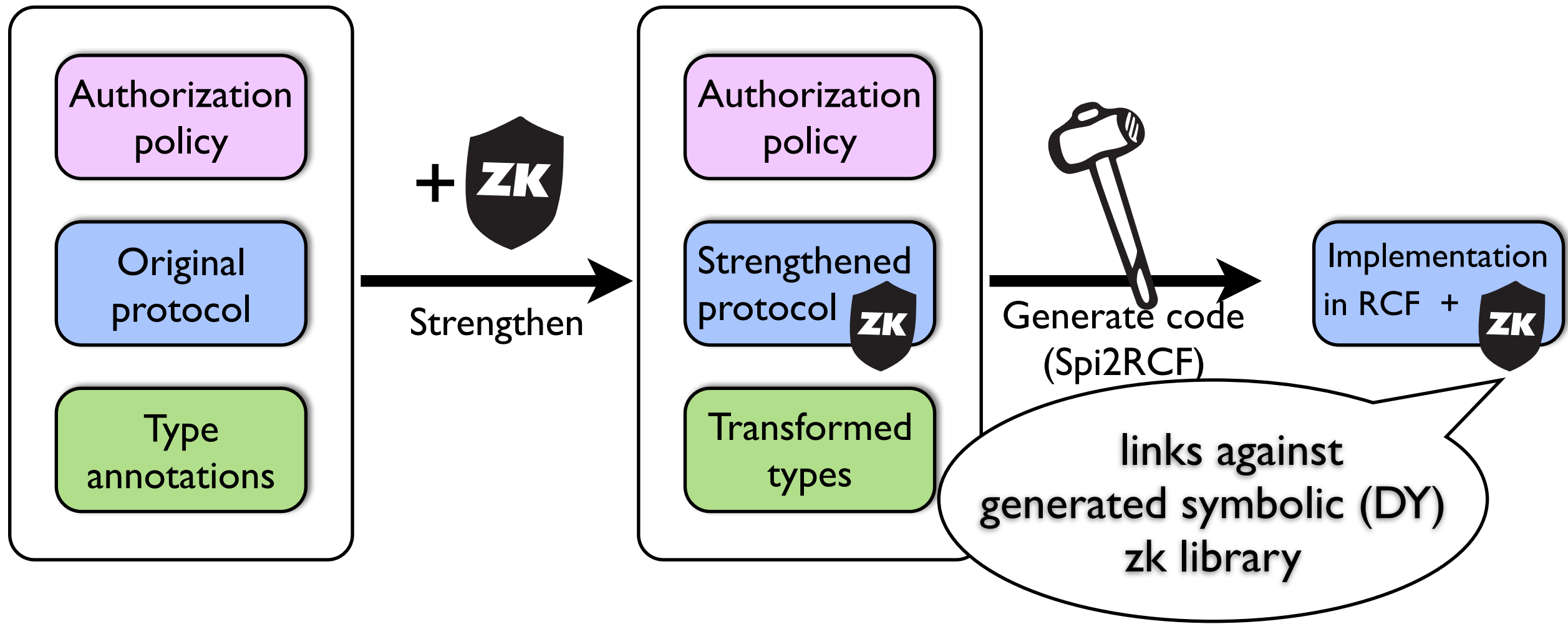


# Automatic code generation



[Bengtson et. al., CSF '08]

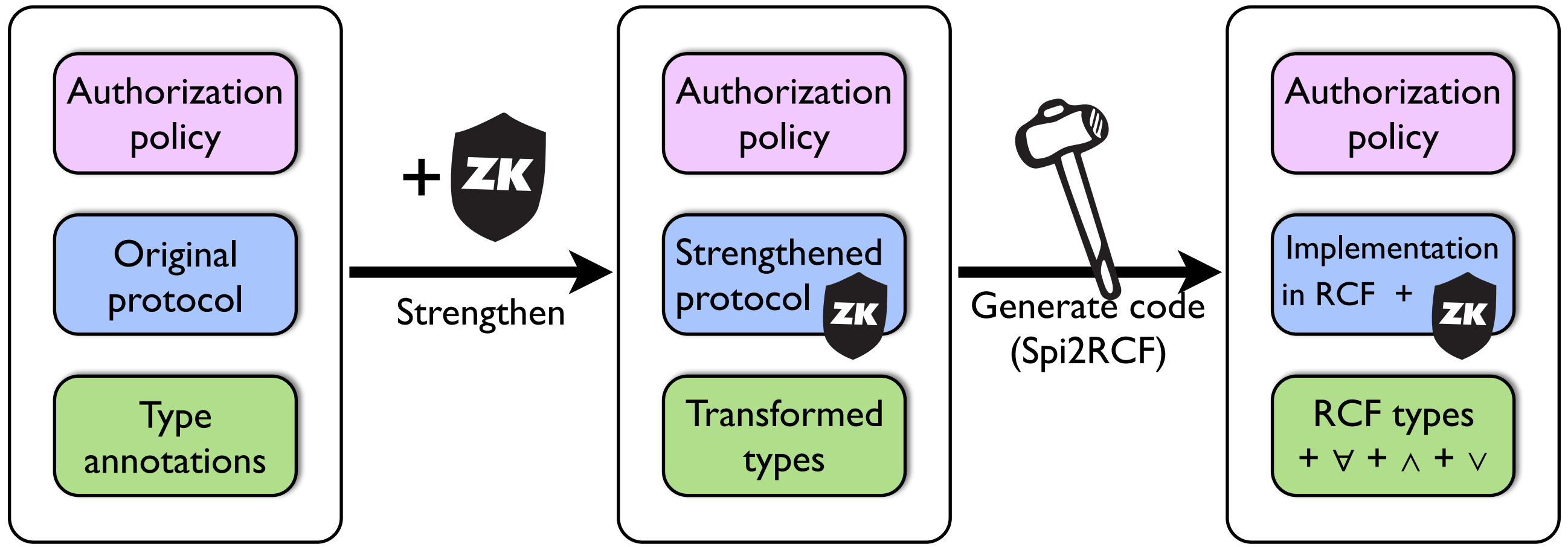
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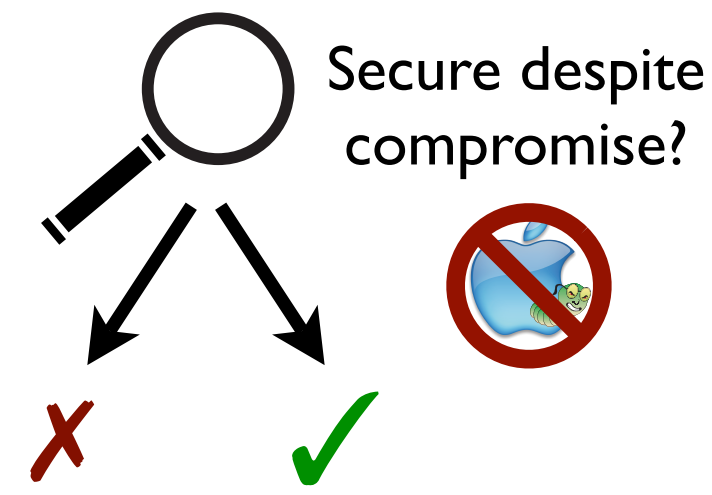
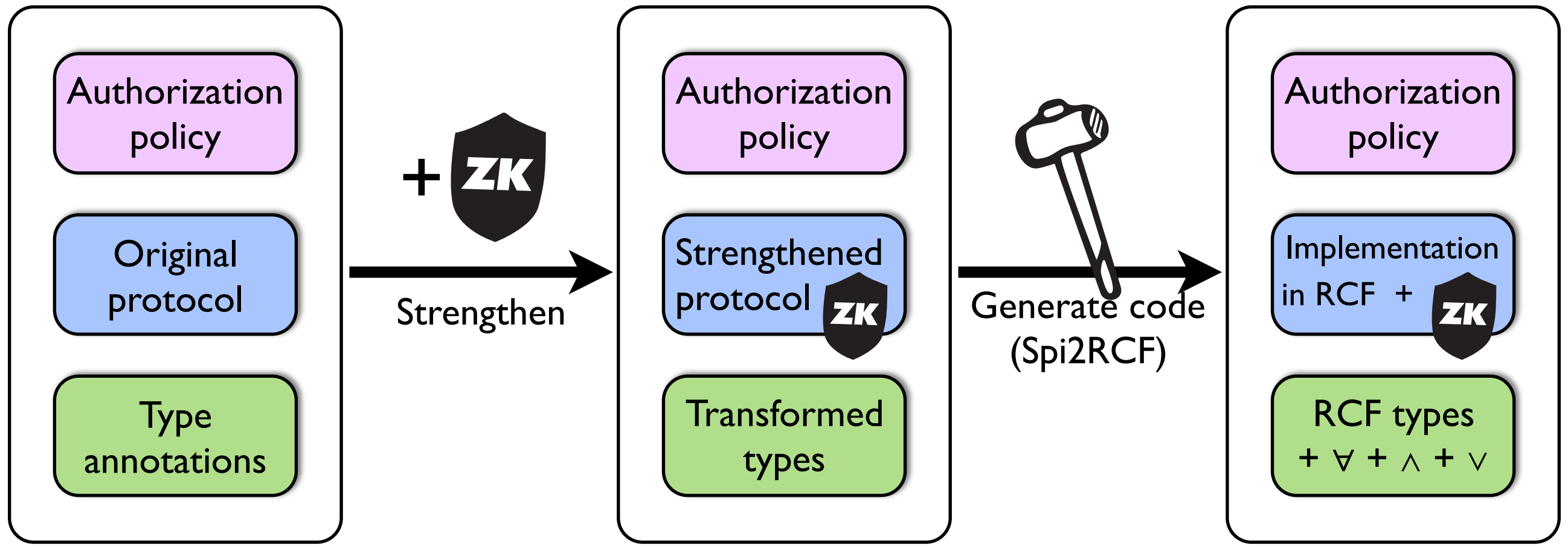
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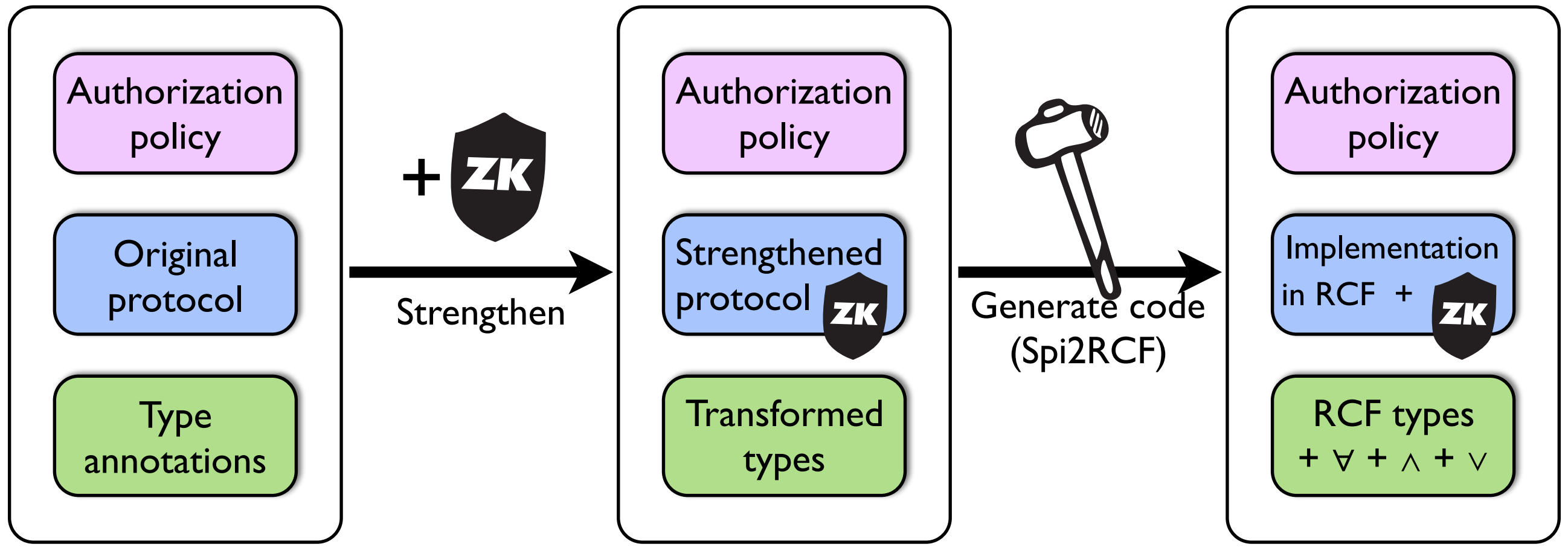
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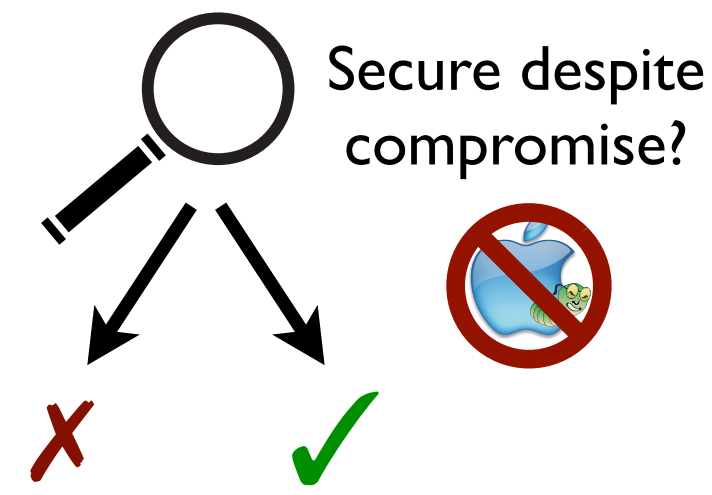
[Bengtson et. al., CSF '08]

[Backes, Hritcu, Maffei & Tarrach, FCS '09 in August]

# Automatic code generation



Recent work Matteo presented in the short talks session



[Bengtson et. al., CSF '08]

[Backes, Hritcu, Maffei & Tarrach, FCS '09 in August]

# Future Work

- Apply transformation to more protocols (e.g. web services)
- Optimize transformation
  - leverage authorization policy and types
  - maybe also use ideas from work on multiparty sessions [Corin et. al, CSF '07 & CSF '09]
  - translation validation approach well-suited for this
- Automatically generate zero-knowledge proof system corresponding to abstract statement
  - concrete cryptographic implementation hard to do by hand
  - efficiency is a big challenge

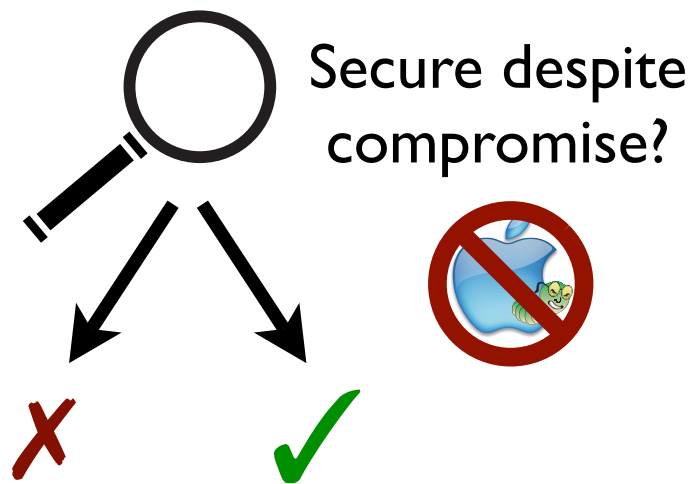
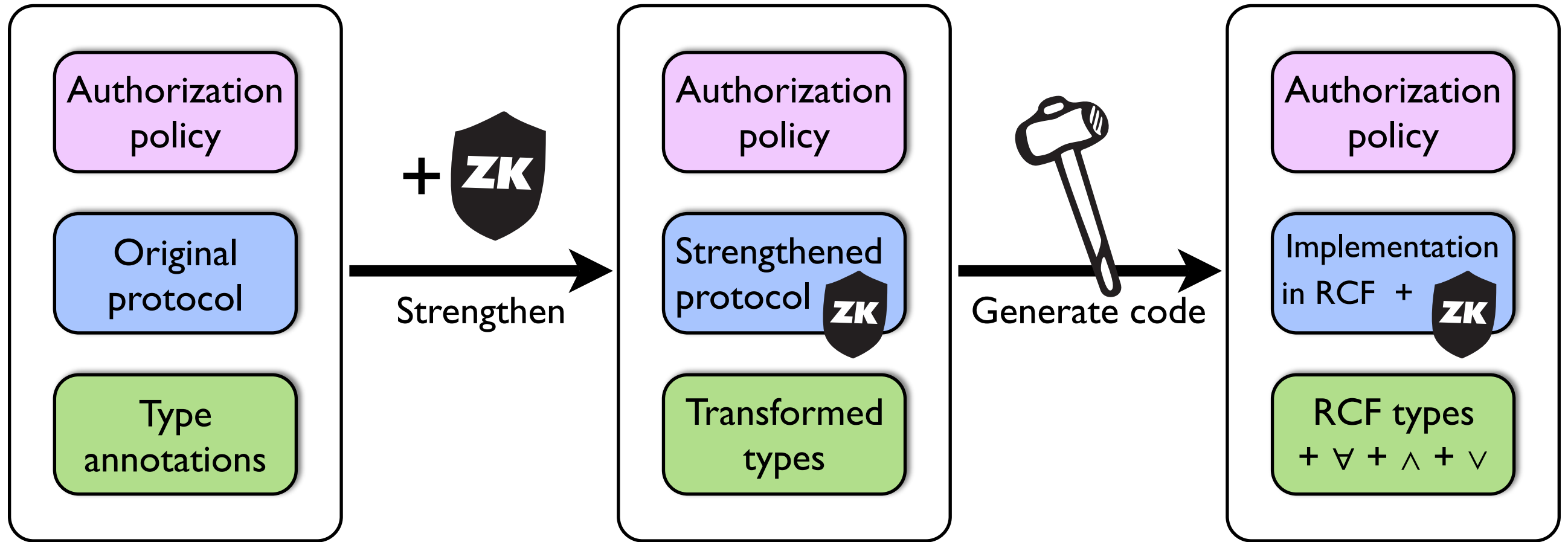




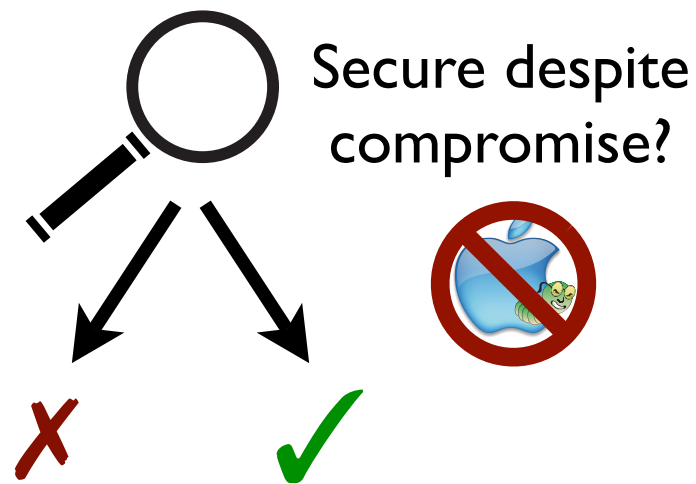
Thank you



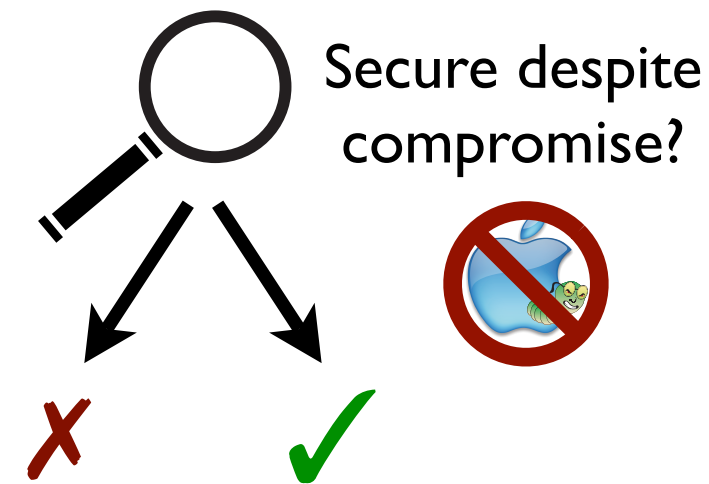
# The big picture



[Fournet, Gordon & Maffei, CSF '07]



[Backes, Hrițcu & Maffei, CCS '08]  
now with  $\wedge + \vee +$  logical kinding



[Bengtson et. al., CSF '08]  
[Backes, Hrițcu, Maffei & Tarrach, FCS '09]

# Related Work

- Strengthening crypto protocols using transformations

[Goldreich, Micali & Wigderson, STOC '87]

- Add ZK to multi-party protocol secure against honest-but-curious participants to protect against compromise
- Computational cryptography, broadcast communication

[Bellare, Canetti & Krawczyk, STOC '98]

- Transformation removes authentication assumption

[Katz & Yung, CRYPTO '03] [Cortier et al. ESORICS '07]

- From passive (eavesdropping) to active attackers

[Datta, Derek, Mitchell & Pavlovic, JCS '05]

- Methodology for modular protocol design using generic protocol transformations

# Related Work (continued)

- Generating protocols from high-level specifications

[Corin, Dénielou, Fournet, Bhargavan & Leifer, CSF '07 & CSF '09]

- Multi-party session specifications transformed to F# implementations that are secure despite compromise
- Very efficient generated implementation
- More recent transformation uses F7 type-checker for translation validation (original one was proven correct)
- Main difference
  - Session specifications have no crypto
  - Our approach applies both to existing crypto protocols and to the ones generated from high-level specs (theirs not)

# Translation validation

[Pnueli et al., TACAS '98]

- Accepted technique for increasing user's confidence in complex transformations (e.g. compiler)
  - + prevents incorrect code from being run
  - + strong guarantees if validation succeeds
  - + without the need to prove transformation always correct
  - + guarantees about actual implementation of transformation
  - + changing transformation is very easy (e.g. optimizing)
  - guarantees only for a specific policy (e.g. authorization policy)
  - no guarantees if validation fails

# Security properties (informal)

- **Robust safety:** in all executions all asserts succeed (i.e. asserts are logically entailed by the active assumes)
  - in the presence of arbitrary DY attacker
  - but where all participants are assumed honest



- **Safety despite compromise:**

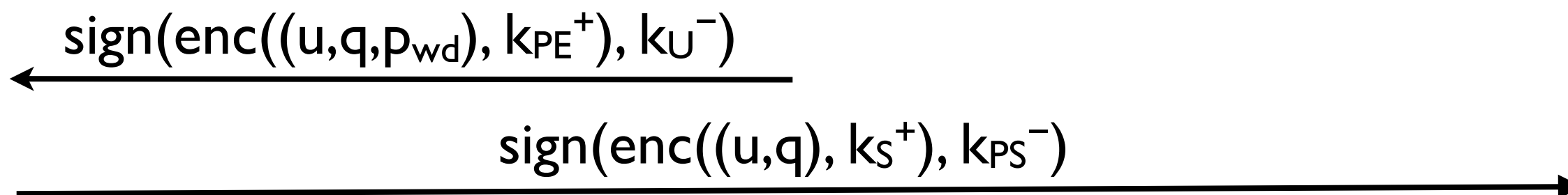
“An invalid authorization decision [...] should only arise if participants on which the decision logically depends are compromised.”

“Hence, the impact of partial compromise should be apparent from the policy, without study of the code”

[Fournet, Gordon & Maffeis, CSF '07]



# Authorization policy



```
let user = new q; assume Request(u, q) |
  out(c1, sign(enc((u,q,pwd), kPE+), kU-)).
```

```
let proxy = assume Registered(u) |
  in(c1, x);
  let (u, xq, pwd) = dec(check(x, kPE-), kPE+);
  out(c2, sign(enc((u,xq), kS+), kPS-)).
```

```
let store = in(c2, z);
  let (xu, xq) = dec(check(z, kPS+), kPS-);
  assert Authenticate(xu, xq).
```

This policy enforces that the store authenticates the user only if a registered user has indeed issued a request

```
let policy = assume  $\forall u, q. (\text{Request}(u, q) \wedge \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q))$ 
```

```
new kU-, kPE-, kPS-, kS-, pwd; (user | proxy | store | policy)
```

# Security despite compromise

[Fournet, Gordon & Maffei, CSF '07]



proxy

**let** user = **new** q; **assume** Request(u, q) |  
     **out**(c<sub>1</sub>, sign(enc((u,q,p<sub>wd</sub>), k<sub>PE</sub><sup>+</sup>), k<sub>U</sub><sup>-</sup>)).

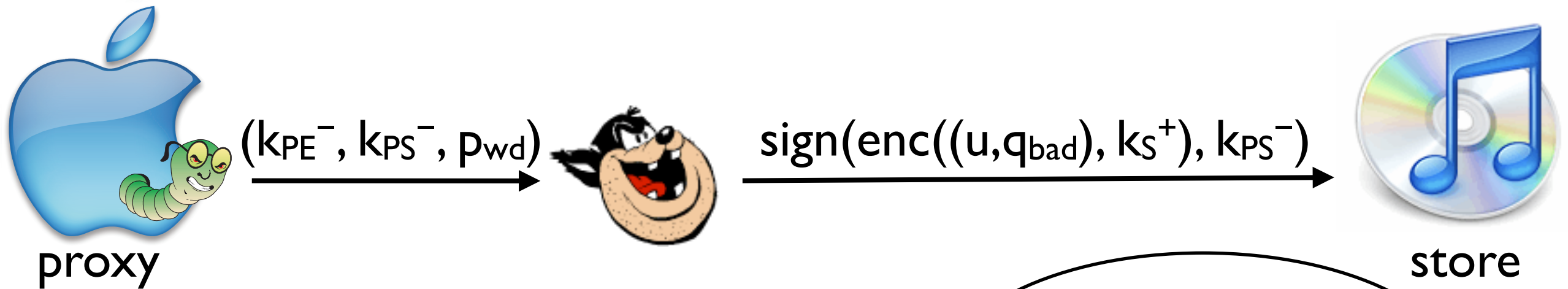
**let** proxy = **assume** Registered(u) |  
     **in**(c<sub>1</sub>, x);  
     **let** (=u, x<sub>q</sub>, =p<sub>wd</sub>) = dec(check(x, k<sub>U</sub><sup>+</sup>), k<sub>PE</sub><sup>-</sup>) **in**  
     **out**(c<sub>2</sub>, sign(enc((u,x<sub>q</sub>), k<sub>S</sub><sup>+</sup>), k<sub>PS</sub><sup>-</sup>)).

**let** store = ...

**let** policy = **assume**  $\forall u, q. (\text{Request}(u, q) \wedge \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q))$  |  
     **assume** Compromised(u)  $\Rightarrow \forall q. \text{Request}(u, q)$  |  
     **assume** Compromised(p)  $\Rightarrow \forall u. \text{Registered}(u)$



# Compromising the proxy



**let** user = **new** q; **assume** Request(u, q) |  
**out**(c<sub>1</sub>, sign(enc((u, q, p<sub>wd</sub>), k<sub>PE</sub><sup>+</sup>), k<sub>U</sub><sup>-</sup>)).

**let** bad\_proxy = **out**(c<sub>pub</sub>, (k<sub>PE</sub><sup>-</sup>, k<sub>PS</sub><sup>-</sup>, p<sub>wd</sub>)).

**let** store = **in**(c<sub>2</sub>, z);  
**let** (x<sub>u</sub>, x<sub>q</sub>) = dec(check(z, k<sub>PS</sub><sup>+</sup>),  
**assert** Authenticate(x<sub>u</sub>, x<sub>q</sub>).

**let** policy = **assume**  $\forall u, q. (\text{Request}(u, q) \wedge \neg \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q))$  |

**assume** Compromised(u)  $\Rightarrow \forall q. \text{Request}(u, q)$  |

**assume** Compromised(p)  $\Rightarrow \forall u. \text{Registered}(u)$

**assume**  $\neg \text{Compromised}(u) \wedge \text{Compromised}(p) \wedge \neg \text{Compromised}(s)$

The transformed  
protocol is

assert fails, so protocol is  
not secure if the proxy is  
compromised

**typedef**  $T_1 = \text{Triple}(x_u : \text{Un}, \{x_q : \text{Un} \mid \text{Request}(x_u, x_q)\}, x_p : \text{Private})$

**typedef**  $T_2 = \text{Pair}(x_u : \text{Un}, \{x_q : \text{Un} \mid \text{Request}(x_u, x_q) \wedge \text{Registered}(x_u)\})$

**let** user = **new** q : Un; **assume** Request(u, q) |  
**out**(c<sub>1</sub>, sign(enc((u,q,p<sub>wd</sub>), k<sub>PE</sub><sup>+</sup>), k<sub>U</sub><sup>-</sup>)).

**let** proxy' = **assume** Registered(u) |  
**in**(c<sub>1</sub>, x);  
**let** (u, x<sub>q</sub>, p<sub>wd</sub>) = dec(check(x, k<sub>U</sub><sup>+</sup>), k<sub>PE</sub><sup>-</sup>) **in**  
**out**(c<sub>2</sub>, zk<sub>S</sub>(k<sub>PE</sub><sup>-</sup>, x<sub>q</sub>, p<sub>wd</sub>; sign(enc((u,x<sub>q</sub>), k<sub>S</sub><sup>+</sup>), k<sub>PS</sub><sup>-</sup>), x, u).

**let** store' = **in**(c<sub>2</sub>, z);  
**let** (β<sub>1</sub>, β<sub>2</sub>, β<sub>3</sub>) = ver<sub>S</sub>(z) **in**  
**let** (x<sub>u</sub>, x<sub>q</sub>) = dec(check(β<sub>1</sub>, k<sub>PS</sub><sup>+</sup>), k<sub>S</sub><sup>-</sup>) **in**  
**assert** Authenticate(x<sub>u</sub>, x<sub>q</sub>).

**let** policy = **assume**  $\forall u, q. (\text{Request}(u, q) \wedge \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q)) \dots$

**new** k<sub>U</sub><sup>-</sup> : SigKey(PubEnc(T<sub>1</sub>));

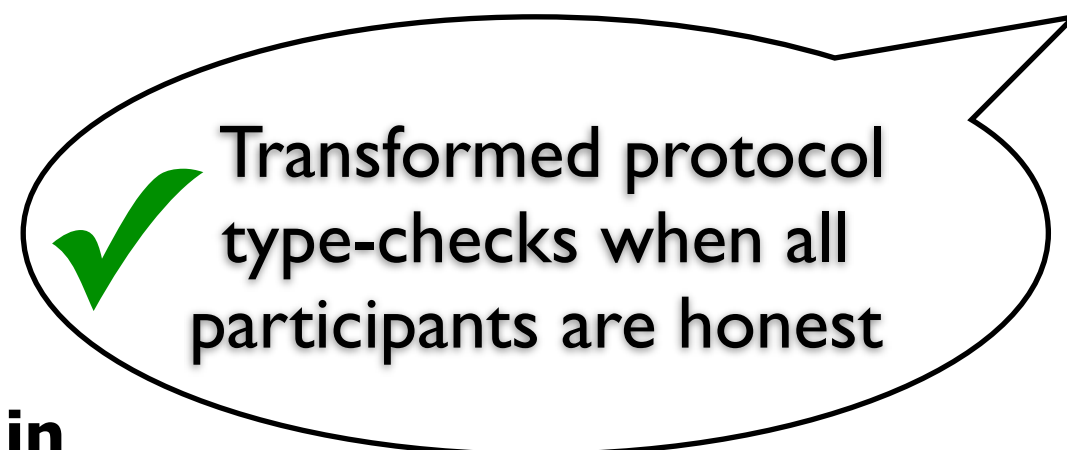
**new** k<sub>PE</sub><sup>-</sup> : DecKey(T<sub>1</sub>);

**new** p<sub>wd</sub> : Private ;

(user | proxy' | store' | policy)

**new** k<sub>PS</sub><sup>-</sup> : SigKey(PubEnc(T<sub>2</sub>)) ;

**new** k<sub>S</sub><sup>-</sup> : DecKey(T<sub>2</sub>) ;



```

typedef T1 = Triple(xu : Un, {xq : Un | Request(xu, xq)}, xp : Private)
typedef T2 = Pair(xu : Un, {xq : Un | Request(xu, xq) ∧ Registered(xu)})

```

```

let user = new q : Un; assume Request(u, q) |
  out(c1, sign(enc((u,q,pwd), kPE+), kU-)).

```

```

let proxy' = assume Registered(u) |
  in(c1, x);
  let (u, xq, pwd) = dec(check(x, kU+), kPE-) in
  out(c2, zkS(kPE-, xq, pwd; sign(enc((u,xq), kS+), kPS-), x, u).

```

But these annotations  
are not appropriate when  
proxy is compromised

```

let store' = in(c2, z);
  let (β1, β2, β3) = verS(z) in
  let (xu, xq) = dec(check(β1, kPS+), kS-) in
  assert Authenticate(xu, xq).

```

```

let policy = assume ∃ u, q. (Request(u, q) ∧ Registered(u) ⇒ Authenticate(u, q)) ...

```

```

new kU- : SigKey(PubEnc(T1));           new kPS- : SigKey(PubEnc(T2))           ;
new kPE- : DecKey(T1);                   new kS- : DecKey(T2)           ;
new pwd : Private           ;
(user | proxy' | store' | policy)

```

**typedef** PrivateUnlessP = {Private |  $\neg$ Compromised(p)}  $\vee$  {Un | Compromised(p)}

**typedef** T<sub>1</sub> = Triple(x<sub>u</sub> : Un, {x<sub>q</sub> : Un | Request(x<sub>u</sub>, x<sub>q</sub>)}, x<sub>p</sub> : PrivateUnlessP)

**typedef** T<sub>2</sub> = Pair(x<sub>u</sub> : Un, {x<sub>q</sub> : Un | Request(x<sub>u</sub>, x<sub>q</sub>)  $\wedge$  Registered(x<sub>u</sub>)})

**typedef** T<sub>2</sub>unlessP = {T<sub>2</sub> |  $\neg$ Compromised(p)}  $\vee$  {Un | Compromised(p)}

**let** user = **new** q : Un; **assume** Request(u, q) |  
**out**(c<sub>1</sub>, sign(enc((u,q,p<sub>wd</sub>), k<sub>PE</sub><sup>+</sup>), k<sub>U</sub><sup>-</sup>)).

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**let** (x<sub>u</sub>, x<sub>q</sub>) = dec(check(β<sub>1</sub>, k<sub>PS</sub><sup>+</sup>), k<sub>S</sub><sup>-</sup>) **in**  
**assert** Authenticate(x<sub>u</sub>, x<sub>q</sub>).

Type of keys does  
not help if proxy  
compromised

**let** policy = **assume**  $\forall u, q. (\text{Request}(u, q) \wedge \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q)) \dots$   
**assume** Compromised(p).

**new** k<sub>U</sub><sup>-</sup> : SigKey(PubEnc(T<sub>1</sub>));

**new** k<sub>PE</sub><sup>-</sup> : DecKey(T<sub>1</sub>);

**new** p<sub>wd</sub> : PrivateUnlessP;

(user | bad\_proxy | store' | policy)

**new** k<sub>PS</sub><sup>-</sup> : SigKey(PubEnc(T<sub>2</sub>unlessP));

**new** k<sub>S</sub><sup>-</sup> : DecKey(T<sub>2</sub>unlessP);

...  
**typedef** T<sub>1</sub> = Triple(x<sub>u</sub> : Un, {x<sub>q</sub> : Un | Request(x<sub>u</sub>, x<sub>q</sub>)}, x<sub>p</sub> : PrivateUnlessP)  
 ...

$$\exists \alpha_1, \alpha_2, \alpha_3. \text{check}(\beta_1, k_{PS}^+) = \text{enc}((\beta_3, \alpha_2), k_S^+) \wedge \text{dec}(\text{check}(\beta_2, k_U^+), \alpha_1) = (\beta_3, \alpha_2, \alpha_3) \wedge \text{Request}(x_u, x_q)$$



Transformed protocol type-checks  
 even when proxy is compromised  
 $\Rightarrow$  secure despite compromise

**let** store' = **in**(c<sub>2</sub>, z);  
**let** (β<sub>1</sub>, β<sub>2</sub>, β<sub>3</sub>) = **vers**<sub>s</sub>(z) **in**  
**let** (x<sub>u</sub>, x<sub>q</sub>) = **dec**(**check**(β<sub>1</sub>, k<sub>PS</sub><sup>+</sup>), k<sub>S</sub><sup>-</sup>) **in**  
**assert** Authenticate(x<sub>u</sub>, x<sub>q</sub>).

**let** policy = **assume**  $\forall u, q. (\text{Request}(u, q) \wedge \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q)) \dots$   
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**new** k<sub>PE</sub><sup>-</sup> : DecKey(T<sub>1</sub>);

**new** p<sub>wd</sub> : PrivateUnlessP;

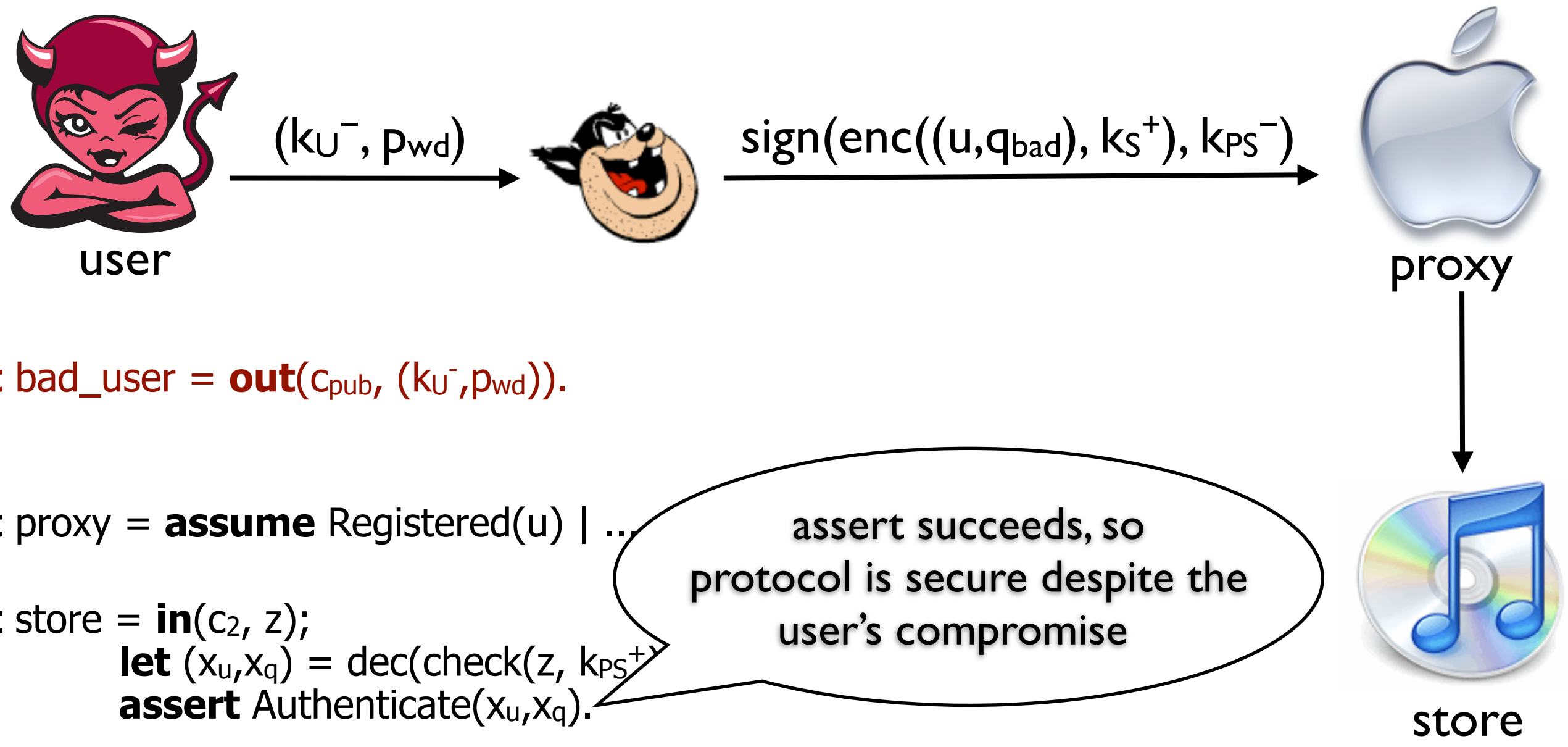
(user | bad\_proxy | store' | policy)

**new** k<sub>PS</sub><sup>-</sup> : SigKey(PubEnc(T<sub>2</sub>unlessP));

**new** k<sub>S</sub><sup>-</sup> : DecKey(T<sub>2</sub>unlessP);



# Compromising the user



**let** bad\_user = **out**( $c_{\text{pub}}, (k_U^-, p_{wd})$ ).

**let** proxy = **assume** Registered(u) | ...

**let** store = **in**( $c_2, z$ );  
**let** ( $x_u, x_q$ ) = **dec**(**check**( $z, k_{PS}^+$ ));  
**assert** **Authenticate**( $x_u, x_q$ ).

**let** policy = **assume**  $\forall u, q. (\text{Request}(u, q) \wedge \text{Registered}(u) \Rightarrow \text{Authenticate}(u, q))$  |

**assume**  $\text{Compromised}(u) \Rightarrow \forall q. \text{Request}(u, q)$  |

**assume**  $\text{Compromised}(p) \Rightarrow \forall u. \text{Registered}(u)$

**assume**  $\text{Compromised}(u) \wedge \neg \text{Compromised}(p) \wedge \neg \text{Compromised}(s)$

```

typedef PrivateUnlessP = {Private | ¬Compromised(p)} ∨ {Un | Compromised(p)}
typedef T1 = Triple(xu : Un, {xq : Un | Request(xu, xq)}, xp:PrivateUnlessP)
typedef T2 = Pair(xu : Un, {xq : Un | Request(xu, xq) ∧ Registered(xu)})
typedef T2unlessP = {T2 | ¬Compromised(p)} ∨ {Un | Compromised(p)}
new kU- : SigKey(PubEnc(T1));
new kPE- : DecKey(T1);
new kPS- : SigKey(PubEnc(T2unlessP));
new kS- : DecKey(T2unlessP);
new pwd : Private; (user | proxy | store | policy)

stmt S = check(β1, kPS+) = enc((β3, α2), kS+) ∧ dec(check(β2, kU+), α1) = (β3, α2, α3)

let user = new q : Un; assume Request(u, q) |
    out(c1, sign(enc((u, q), pwd), kPE+), kU-)).

let proxy = assume Registered(u) |
    in(c1, x);
    let (=u, xq, =pwd) = dec(check(x, kU+), kPE-) in
    out(c2, sign(enc((u, xq), kS+), kPS-)).

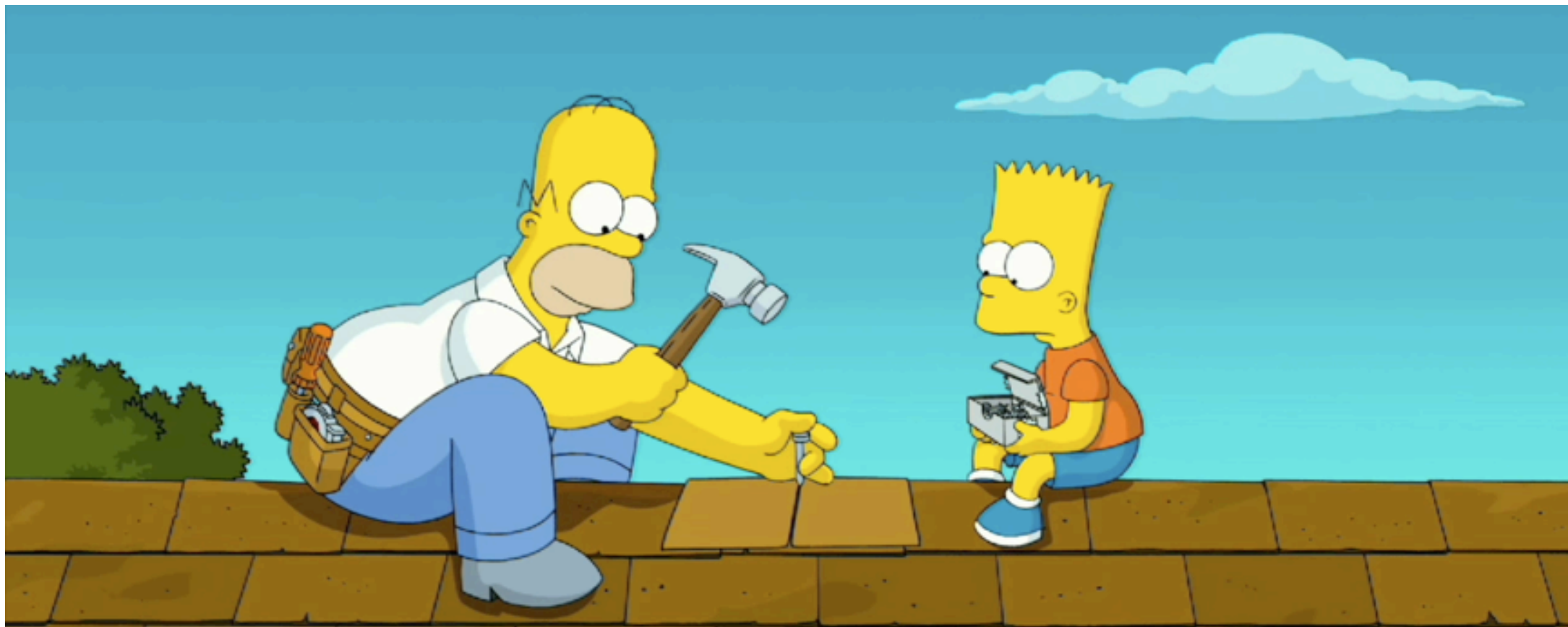
let store = in(c2, z);
    let (xu, xq) = dec(check(z, kPS+), kS-) in
    assert Authenticate(xu, xq).

let policy = assume ∃ u, q. (Request(u, q) ∧ Registered(u) ⇒ Authenticate(u, q)) |
    assume Compromised(p) ⇒ ∃ u. Registered(u) |
    assume Compromised(u) ⇒ ∃ q. Request(u, q).

```

# Implementation

- Transformation and type-checker written in O'Cam1 (~2000+6000 LOC)
- Both available under the Apache License:  
<http://www.infsec.cs.uni-sb.de/projects/zk-compromise/>  
<http://www.infsec.cs.uni-sb.de/projects/zk-typechecker/>
- Spi2RCF release coming soon





Thank you

