

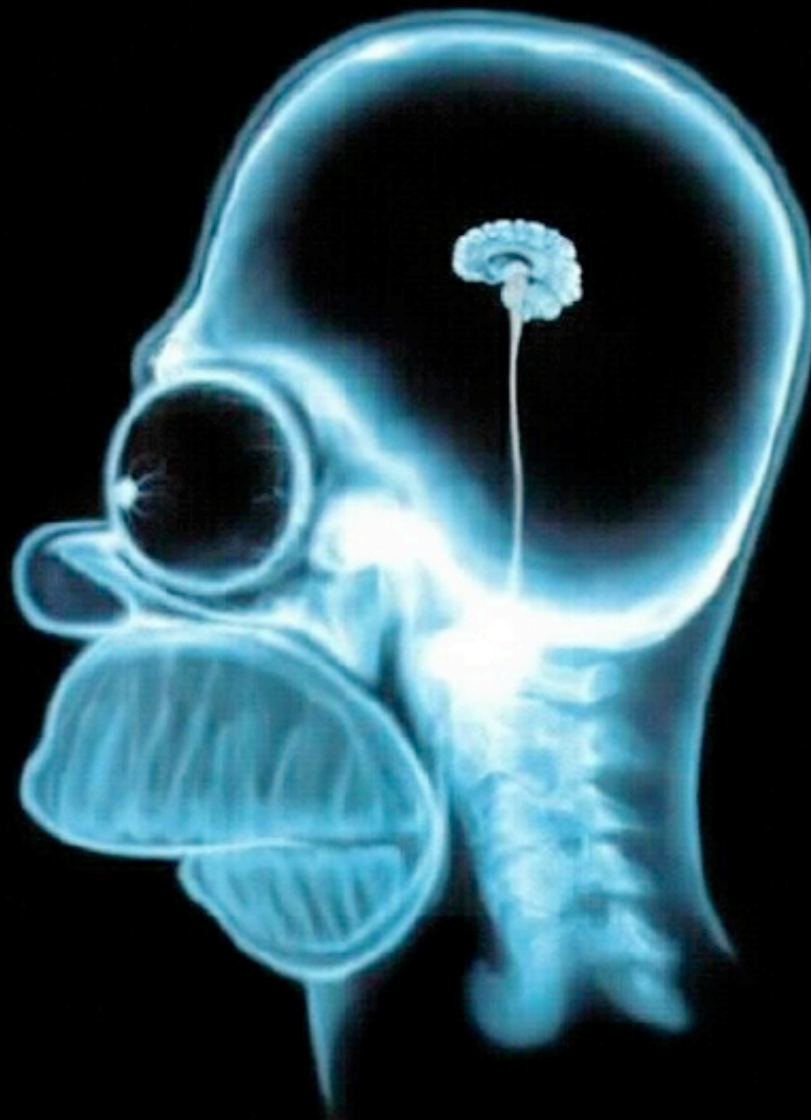
Type-checking Zero-knowledge

Cătălin Hrițcu

Saarland University, Saarbrücken, Germany

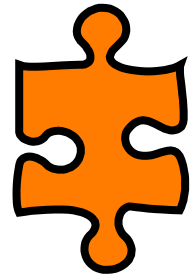
Joint work with: Michael Backes and Matteo Maffei

Zero-knowledge

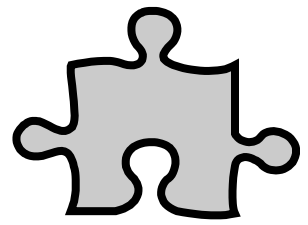


Security Protocols

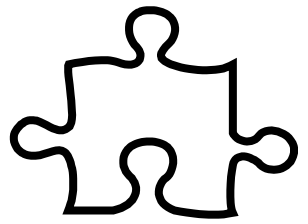
designer's toolbox



hash



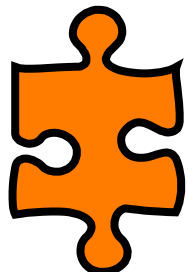
encryption



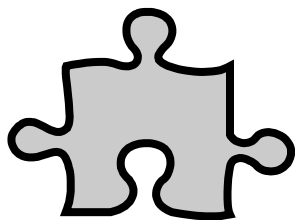
signature

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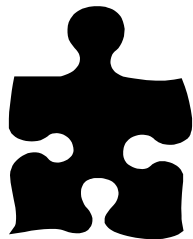
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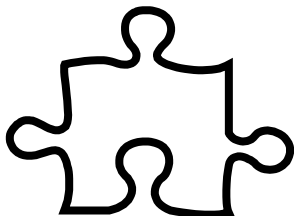
hash



encryption



zero-knowledge



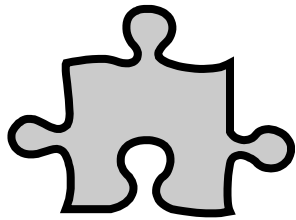
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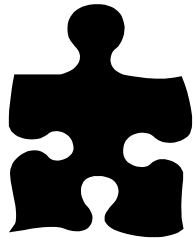
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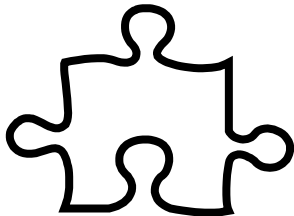
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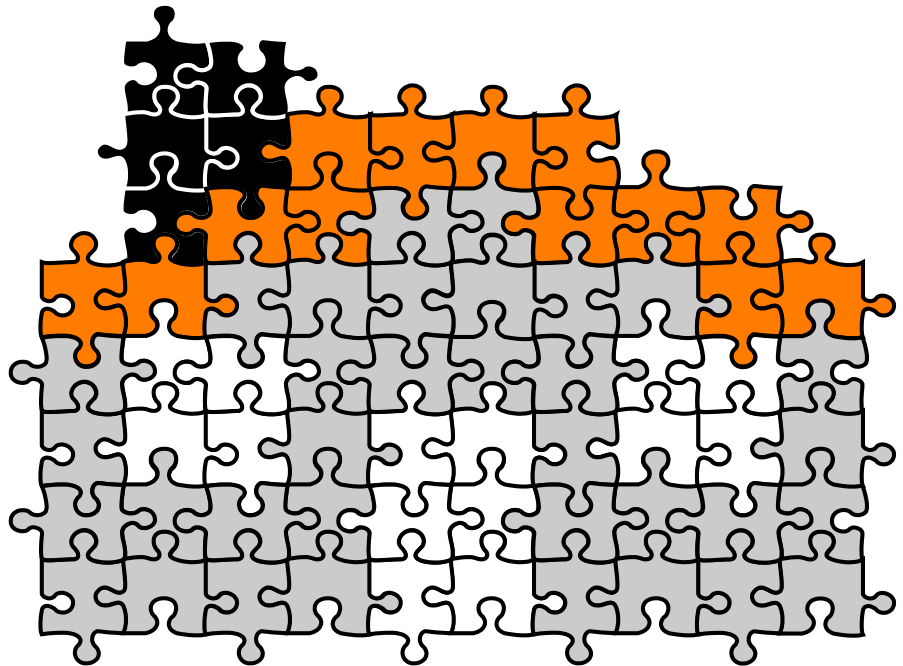
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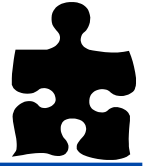
zero-knowledge



signature



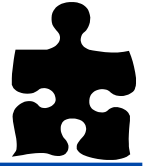
Zero-knowledge Proofs



▶ Powerful primitives

- Prove the validity of a statement without revealing anything else
 - For instance, prove to know an object with certain properties without revealing this witness

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Zero-knowledge Proofs



- ▶ Powerful primitives
 - Prove the validity of a statement without revealing anything else
 - For instance, prove to know an object with certain properties without revealing this witness
- ▶ Early constructions general, but terribly inefficient
 - Very limited practical impact
- ▶ More recent research provided
 - Efficient constructions for special classes of statements
 - Constructions for non-interactive zero-knowledge



e-voting (Civitas)

Applications that use ZK

unique security features of ZK allows
designing protocols fulfilling seemingly
conflicting requirements



“trusted” computing (DAA)



p2p (PseudoTrust)



privacy

+



verifiability



e-voting (Civitas)

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remote attestation



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pseudonymity

+



trust



p2p (PseudoTrust)

Verifying Protocols Using ZK

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Verifying Protocols Using ZK

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- ▶ Our goal
 - *To automatically analyze protocols using ZK in an efficient and scalable way*
- ▶ We built first *type system for zero-knowledge*

Type System

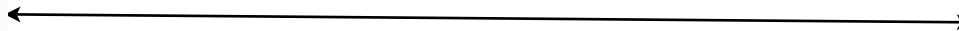
- ▶ Type-checking fully automated and efficient

Type System

- ▶ Type-checking fully automated and efficient
- ▶ Compositional therefore scalable

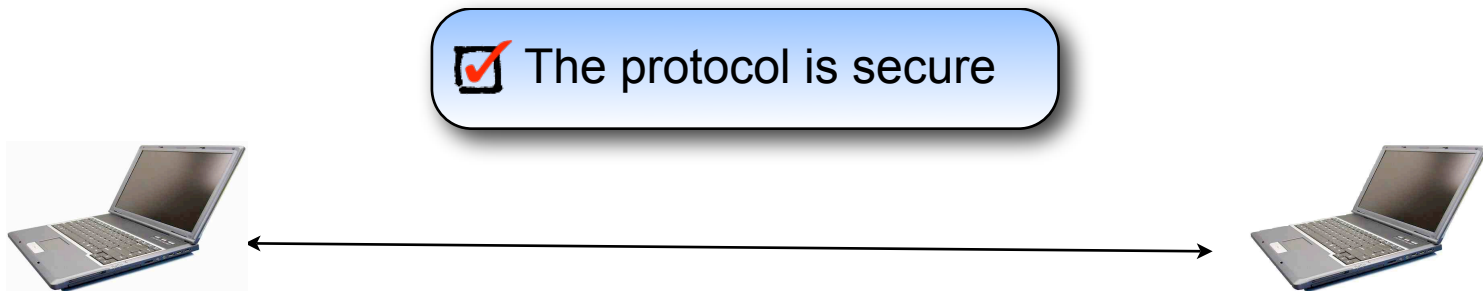
This code is safe

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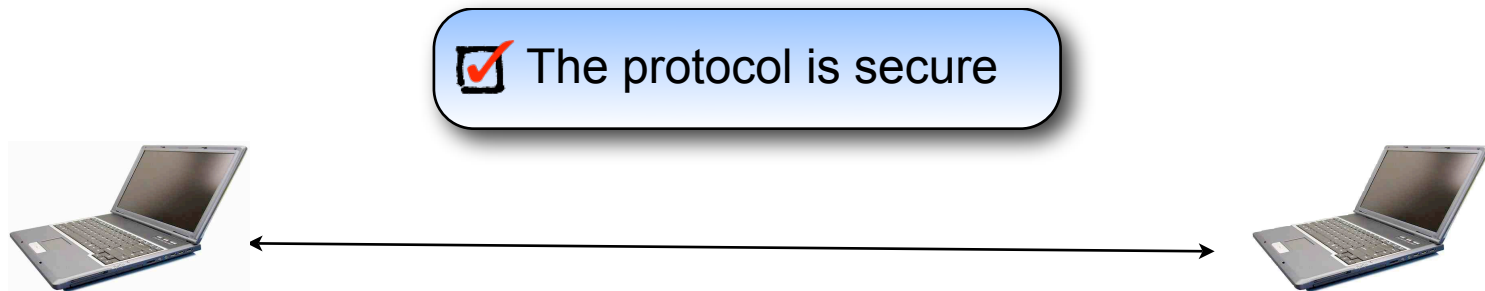
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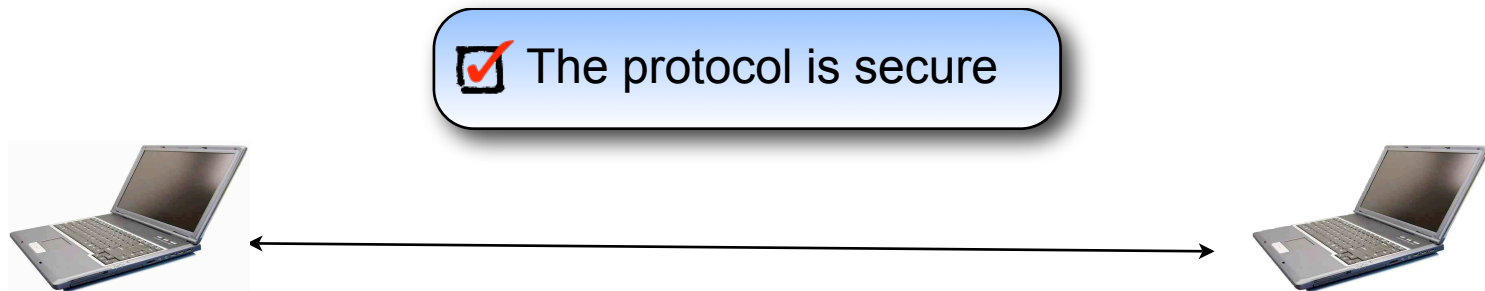
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- ▶ Predictable termination behavior

Type System

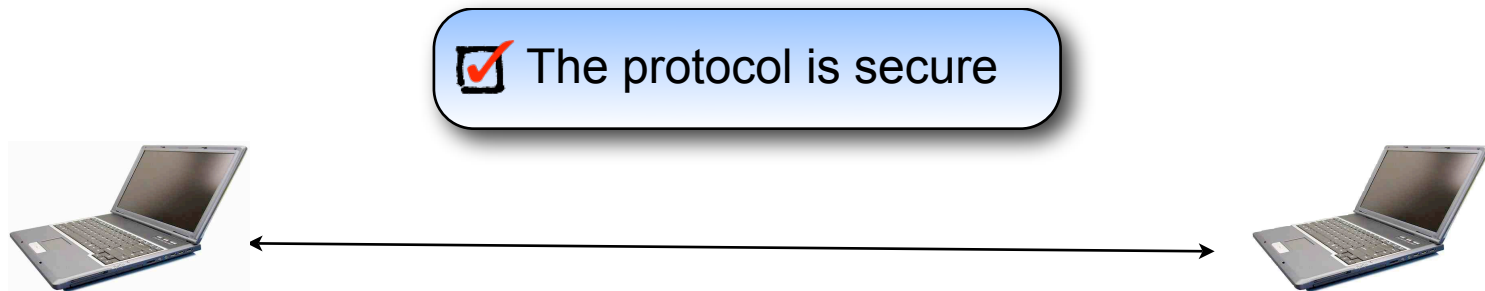
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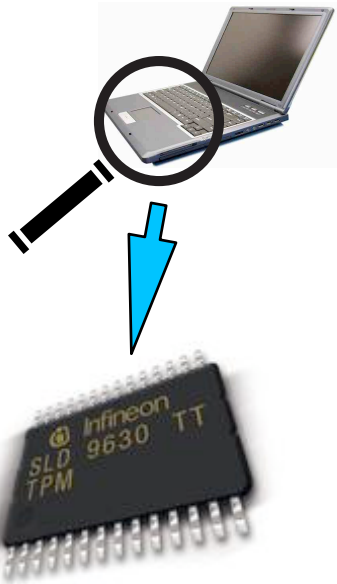


- ▶ Predictable termination behavior
- ▶ User needs to provide annotations (no free lunch)
 - ▶ in certain cases these can be automatically inferred

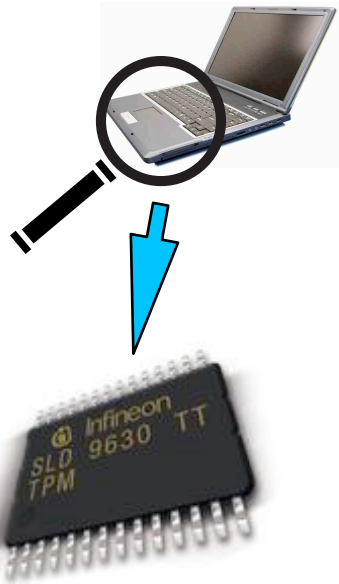
Type-checking DAA

(Direct Anonymous Attestation)

DAA (Direct Anonymous Attestation)

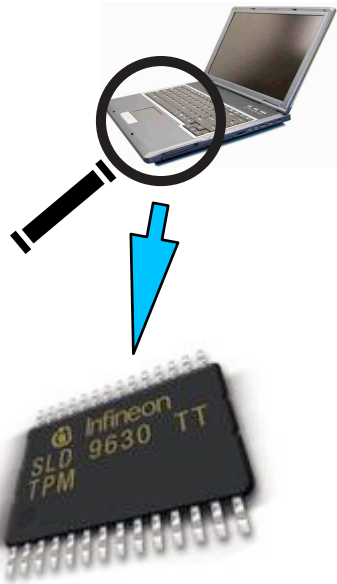


DAA (Direct Anonymous Attestation)



The user wants to authenticate a message m by proving that her platform has a valid TPM inside (*attestation*) ...

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The user wants to authenticate a message m by proving that her platform has a valid TPM inside (*attestation*) ...

... but no other party should learn *which* TPM is used to authenticate m (*anonymity*)

Direct Anonymous Attestation (DAA)



f_{tpm}
(secret TPM identifier)

Issuer



Direct Anonymous Attestation (DAA)



Joining Protocol

The user receives a certificate of f_{tpm} from the issuer

Direct Anonymous Attestation (DAA)



$\text{sign}(f_{\text{tpm}}, k_I)$

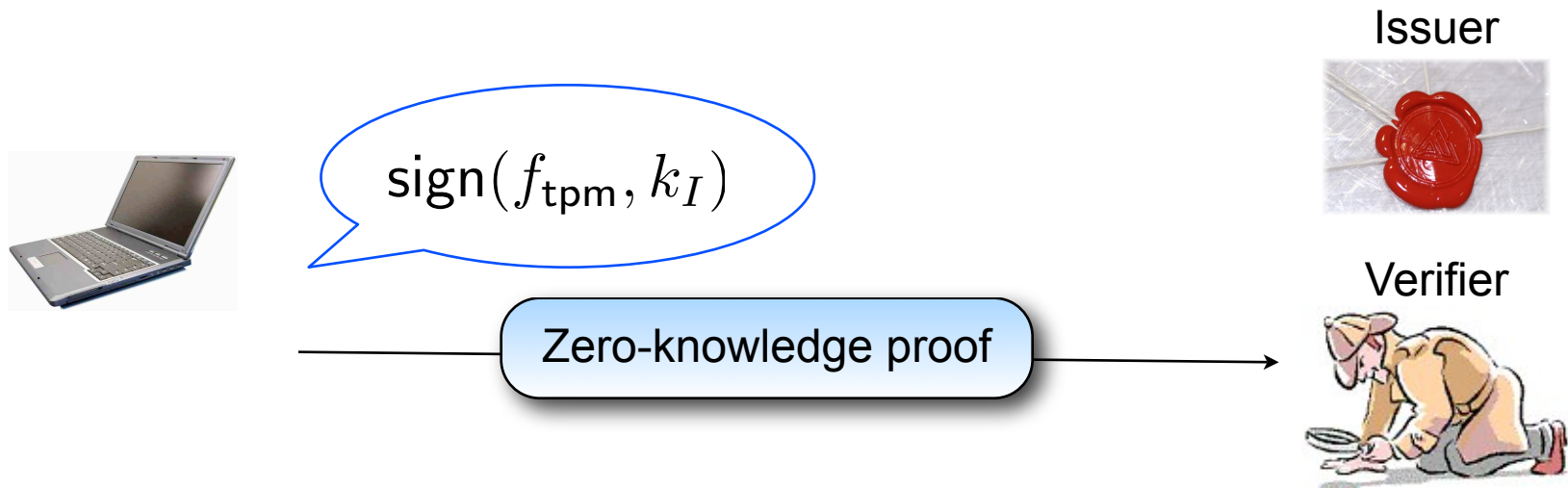
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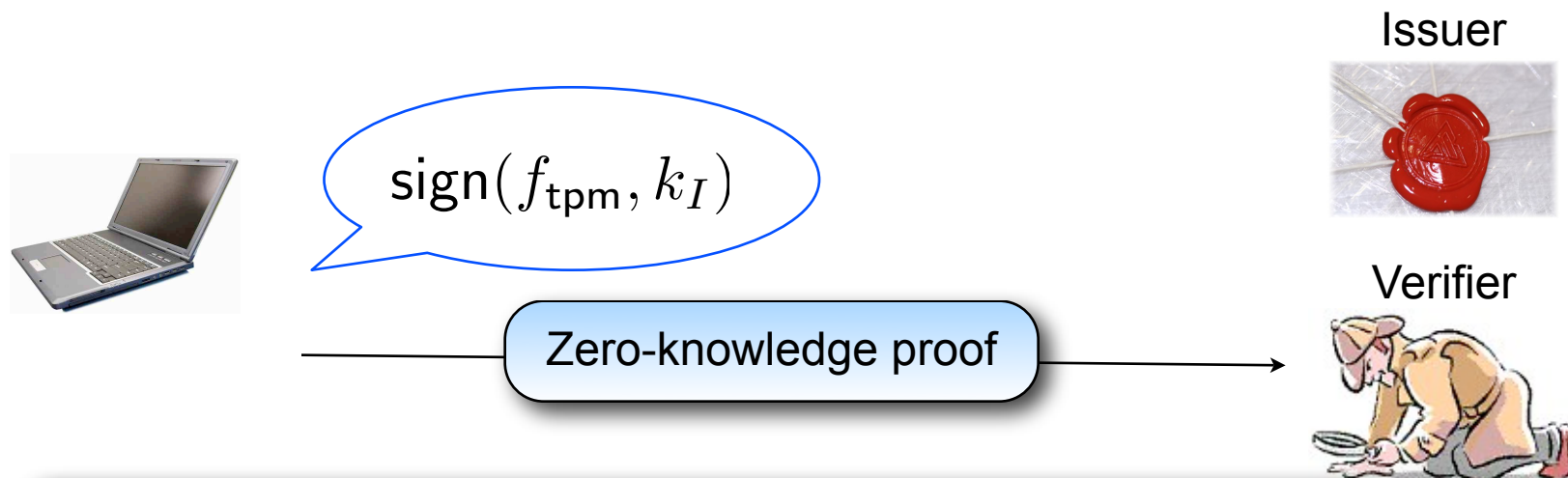
Direct Anonymous Attestation (DAA)



Signing Protocol

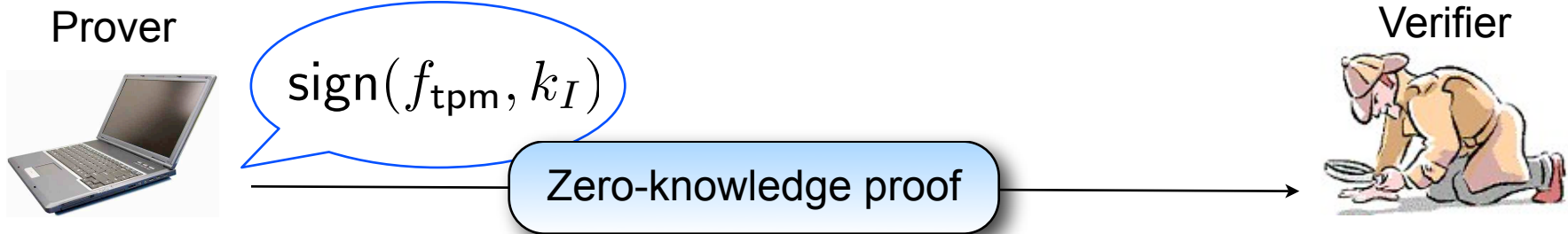
The user proves the knowledge of a certificate for his secret TPM identifier f_{tpm} ... without revealing it!

Direct Anonymous Attestation (DAA)



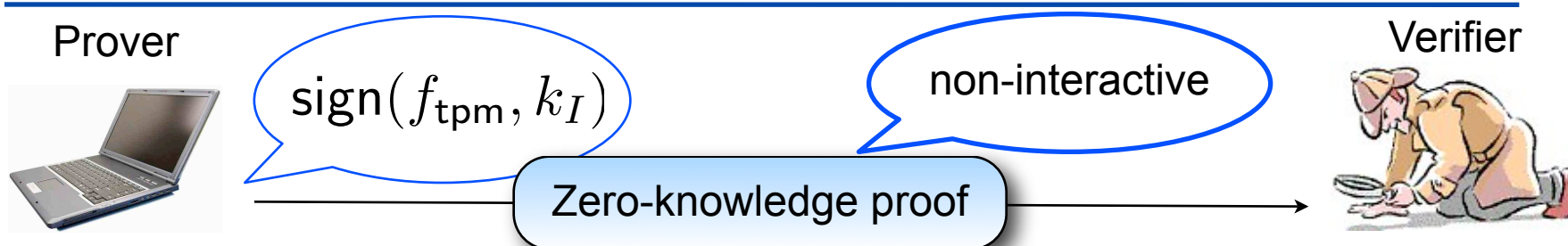
“the user knows a secret identifier and a certificate, and the certificate is a valid signature made by the issuer on the identifier”

Idealization of Zero-knowledge



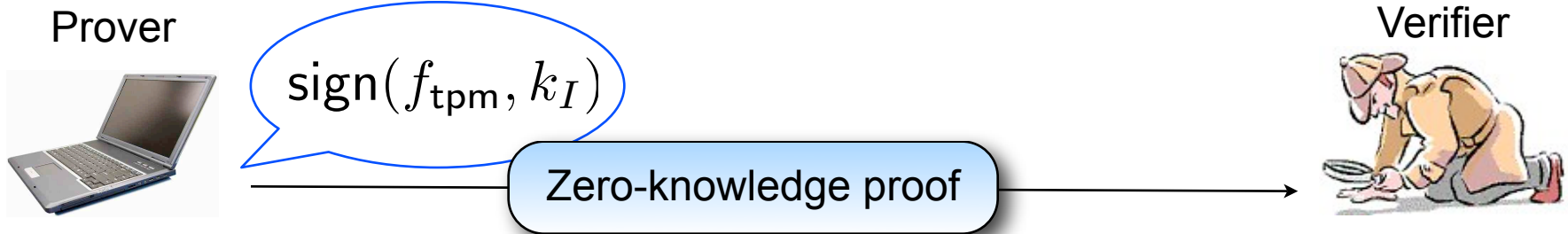
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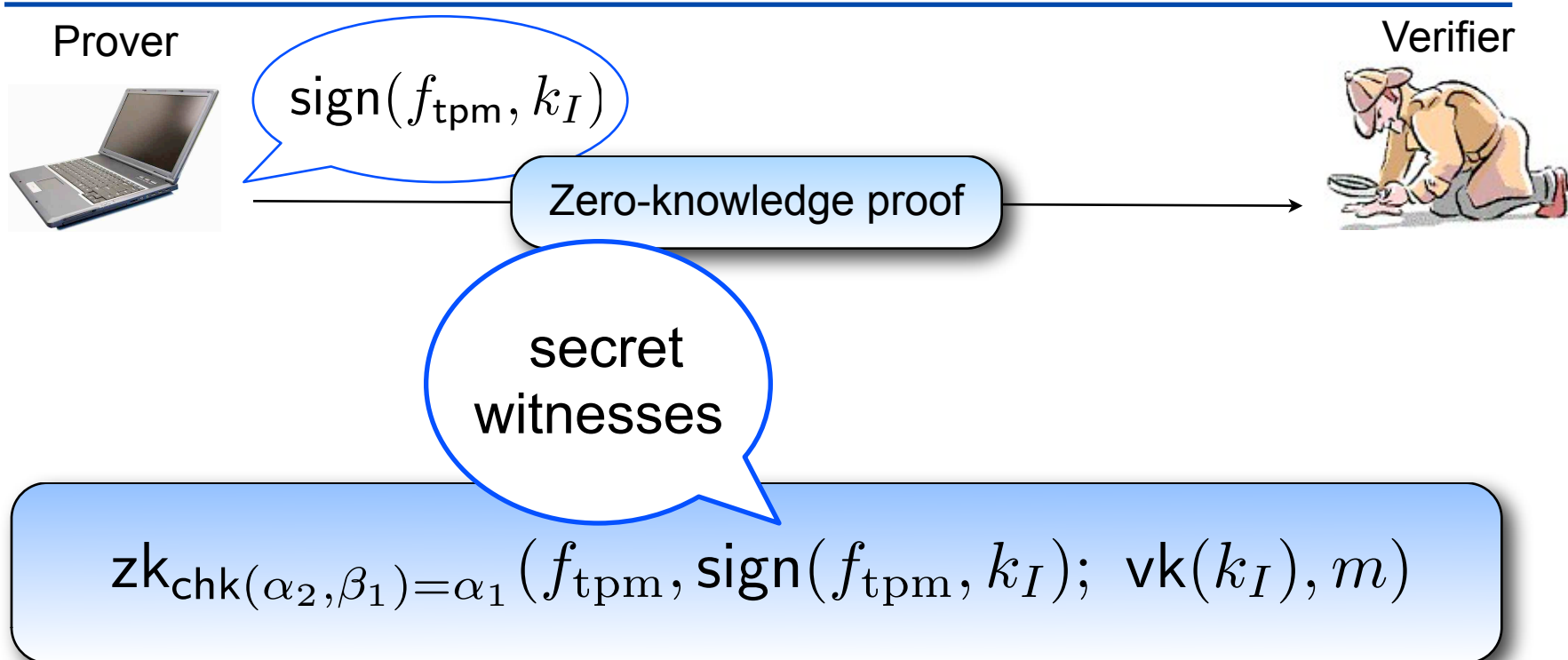
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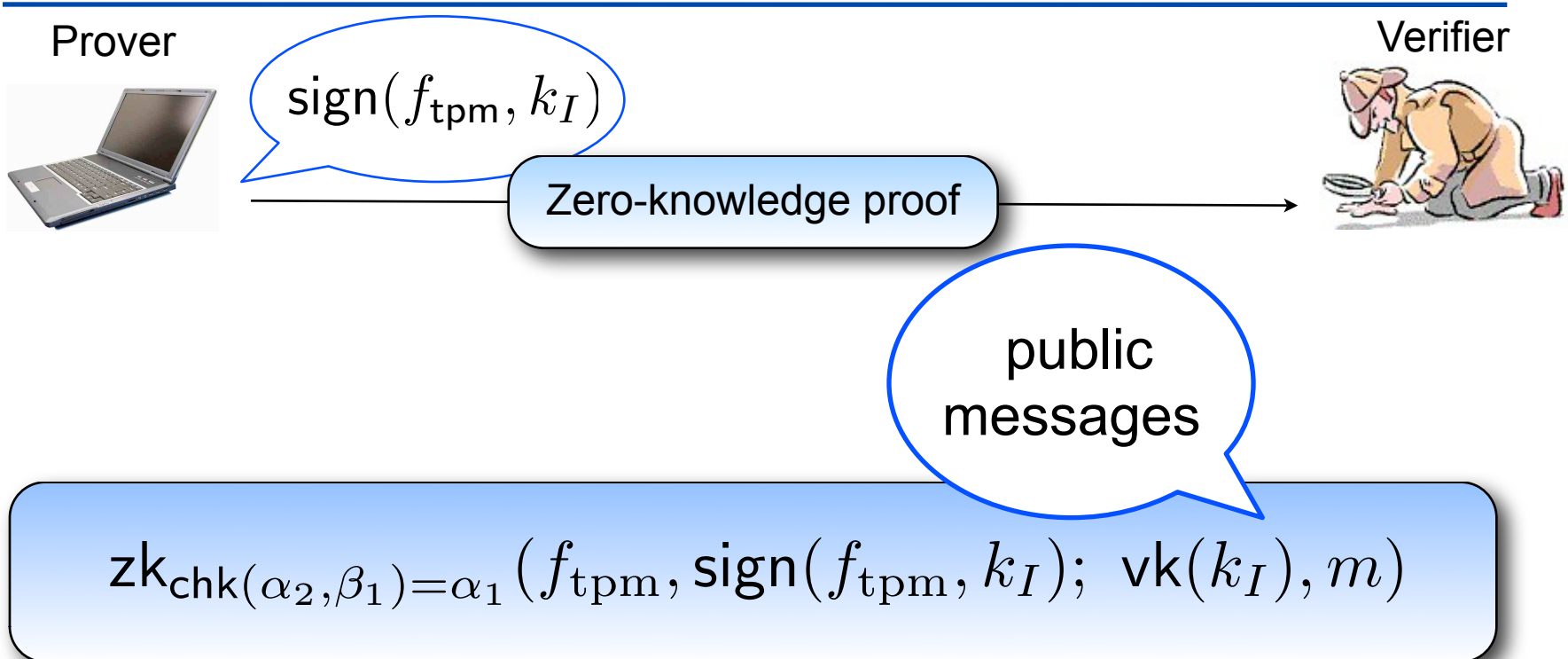


$$\text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m)$$

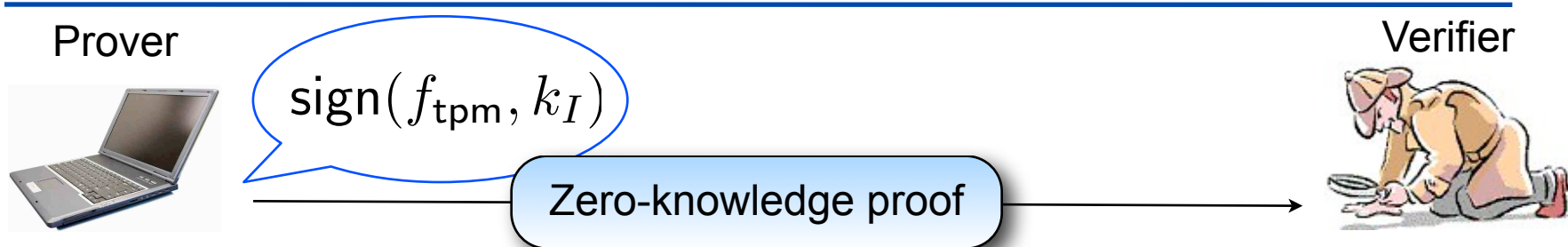
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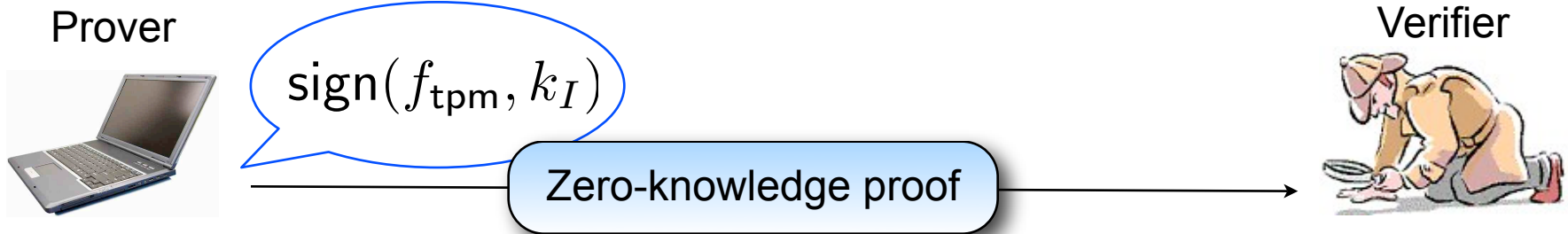


statement

$$\text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m)$$

$$\text{chk}(\alpha_2, \beta_1) = \alpha_1$$

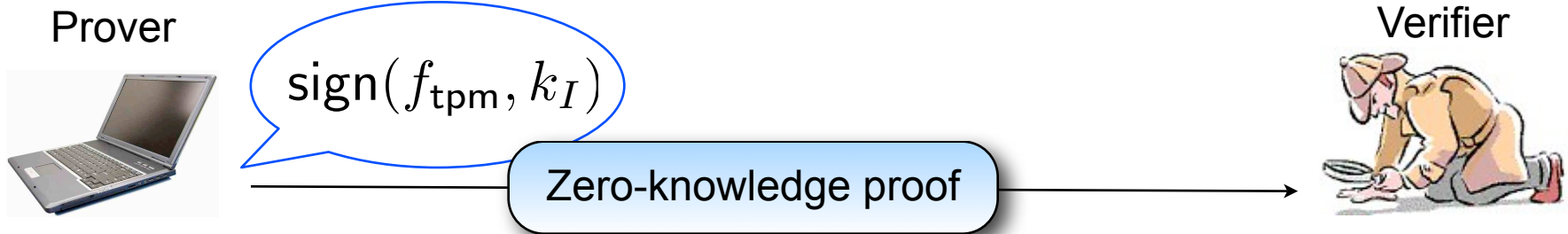
Idealization of Zero-knowledge



$$\text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m)$$

Verification: $\text{chk}(\alpha_2, \beta_1) = \alpha_1$

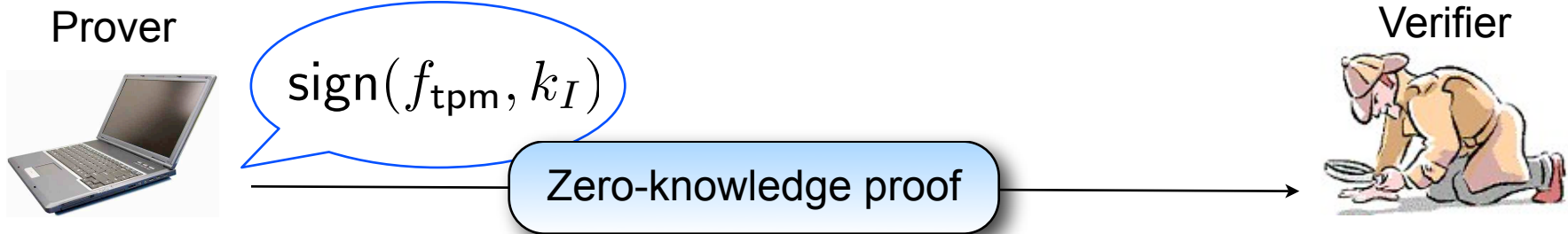
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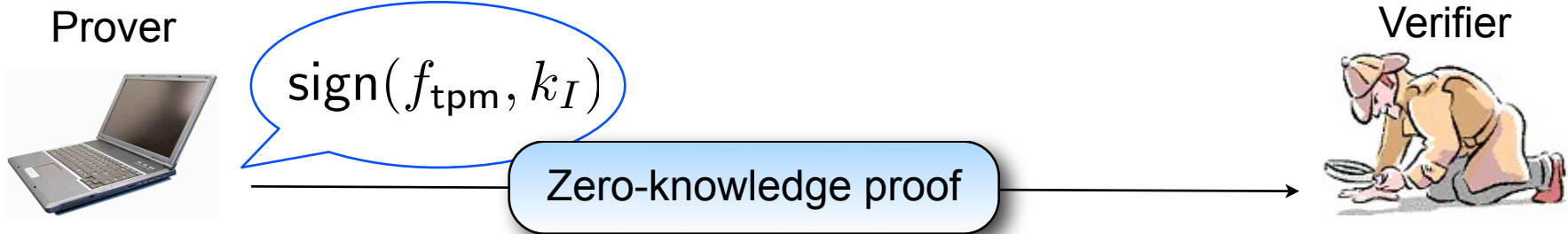
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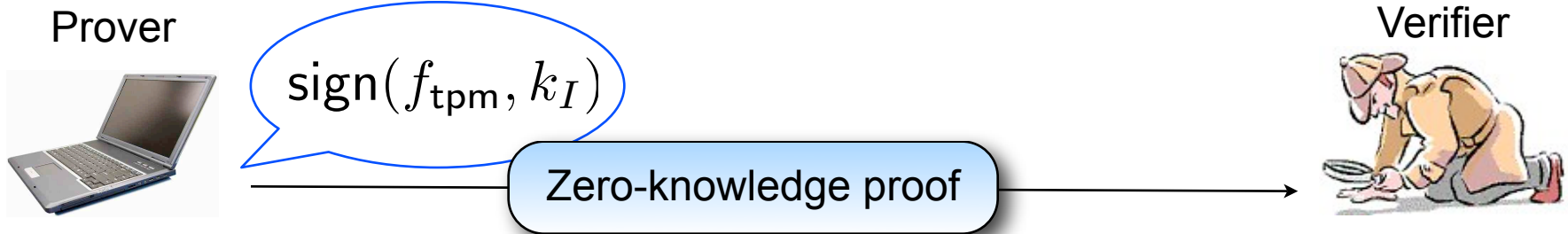
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DAA Signing Protocol (simplified)

Prover



$$zk_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); vk(k_I), m)$$

Verifier



new k_I

new f_{tpm}

Prover | Verifier | Issuer

Prover = new m



$$\text{out}(c, zk_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); vk(k_I), m))$$

Verifier = in(c, x).



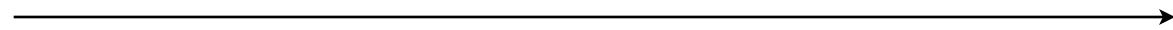
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matching will help typing

Security Annotations

Prover



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Prover | Verifier | Issuer

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assume $\text{Send}(f_{tpm}, m)$ |
 $\text{out}(c, zk_{chk(\alpha_2, \beta_1) = \alpha_1}(f_{tpm}, \text{sign}(f_{tpm}, k_I); vk(k_I), m))$

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Security Annotations

Prover



Verifier



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assume $\forall m. (\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m))$ |

new k_I

new f_{tpm}

Prover | Verifier | Issuer

authorization policy
(in some logic)

Prover = new m



assume $\text{Send}(f_{tpm}, m)$ |

out($c, zk_{chk(\alpha_2, \beta_1) = \alpha_1}(f_{tpm}, \text{sign}(f_{tpm}, k_I); vk(k_I), m)$)

Verifier = in(c, x).



let $y_m = \text{ver}_{chk(\alpha_2, \beta_1) = \alpha_1}(x; vk(k_I))$ then

assert $\text{Authenticate}(y_m)$

Security Annotations

Prover



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assert $\text{Authenticate}(y_m)$

Safety

Asserts are entailed by
the current assumes

Basic Types

assume $\forall m. (\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m))$ |

new k_I

new f_{tpm}

Prover | Verifier | Issuer

Prover = new m



assume $\text{Send}(f_{\text{tpm}}, m)$ |

$\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$

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new k_I

new f_{tpm}

Prover | Verifier | Issuer

Prover = new m : Un



assume $\text{Send}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(m_I); \text{vk}(k_I), m))$

Type of
messages known to
the attacker

Verifier = in(c, x).



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(m_I)$ then
assert $\text{Authenticate}(y_m)$

Basic Types

assume $\forall m. (\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m))$ |

new k_I

new f_{tpm} : Private

Prover | Verifier

Prover = new n



assume $\text{chk}(\alpha_2, \beta_1) = \alpha_1$

out($c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m)$)

Verifier = in(c, x).



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
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Type of messages
unknown to the attacker

Basic Types

assume $\forall m. (\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m))$ |
 new k_I : **SigKey**($\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}$)
 new f_{tpm} : **Private**

Prover | Verifier | Issuer

Prover = new m : **Un**



assume $\text{Send}(f_{\text{tpm}}, m)$ |

out($c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m)$)

Verifier = in(c, x).



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
 assert $\text{Authenticate}(y_m)$

Type of keys used
to sign Private messages for which
OkTPM holds

Basic Types



The type of the key allows us to “transfer” predicates from the prover to the verifier!

assume $\forall m. (\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m))$ |

new $k_I: \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \})$

new $f_{\text{tpm}}: \text{Private}$

Prover | Verifier | Issuer

Prover = new $m: \text{Un}$



assume $\text{Send}(f_{\text{tpm}}, m)$ |

out($c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m)$)

Verifier = in(c, x).



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Basic Types

But, the verifier can't use the key to check a certificate he never receives.

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new f_{tpm} : **Private**

Prover | Verifier | Issuer

Prover = new m : **Un**



assume $\text{Send}(f_{\text{tpm}}, m)$ |

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Basic Types

But, the verifier can't use the key to check a certificate he never receives.

Worse, ZK don't necessarily rely on keys!



assume $\forall m. (\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m))$ |

new k_I : **SigKey**($\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}$)

new f_{tpm} : **Private**

Prover | Verifier | Issuer

Prover = new m : **Un**



assume $\text{Send}(f_{\text{tpm}}, m)$ |

$\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$

Verifier = $\text{in}(c, x)$.



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then

assert $\text{Authenticate}(y_m)$

Typing Zero-knowledge Proofs

Our solution:

User gives a type to each statement proved by ZK

Typing Zero-knowledge Proofs

Prover



$$zk_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); vk(k_I), m)$$

Verifier



$$ZK_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} (\langle y_k : \text{VerKey}(\dots), y_m : \text{Un} \rangle \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \})$$

Typing Zero-knowledge Proofs

Prover



$$zk_{chk(\alpha_2, \beta_1) = \alpha_1}(f_{tpm}, \text{sign}(f_{tpm}, k_I); vk(k_I), m)$$

Verifier



Type of
public messages

$$ZK_{chk(\alpha_2, \beta_1) = \alpha_1} (\langle y_k : \text{VerKey}(\dots), y_m : \text{Un} \rangle \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \})$$

Typing Zero-knowledge Proofs

Prover



$$zk_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); vk(k_I), m)$$

Verifier



$$ZK_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} (\langle y_k : \text{VerKey}(\dots), y_m : \text{Un} \rangle \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \})$$

Logical formula where
the secret witnesses are
existentially quantified

Type-checking the Prover

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

Prover = ...



$\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$

Type-checking the Prover

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$



Type of public messages

Prover =



...
 $\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$

Type-checking the Prover

$$ZK_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \right. \\ \left. \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \right)$$

$\Gamma = \dots$
 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}),$
 $m : \text{Un},$
 \dots
 $\text{OkTPM}(f_{\text{tpm}}),$
 $\text{Send}(f_{\text{tpm}}, m)$

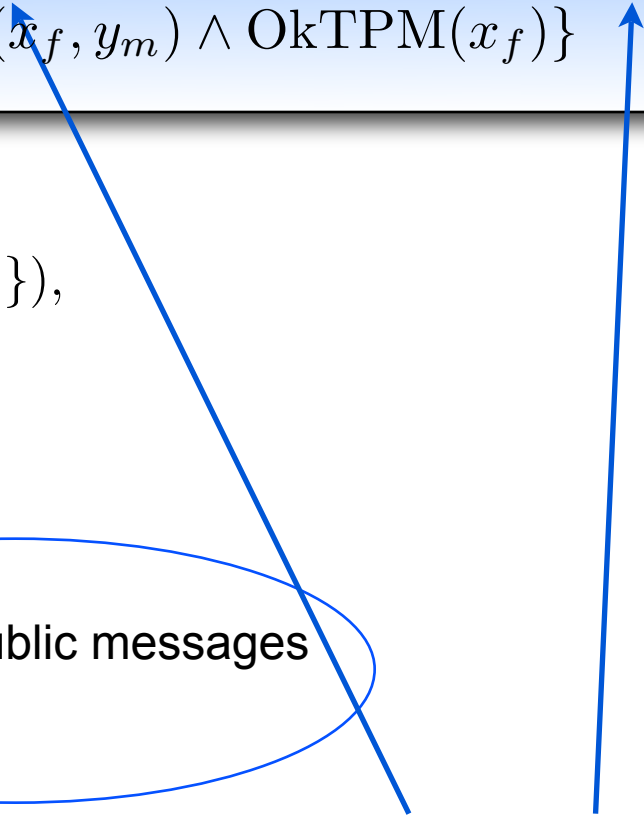


Type of public messages

Prover =



\dots
 $\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$



Type-checking the Prover

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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 \dots
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 $\text{Send}(f_{\text{tpm}}, m)$



- Type of public messages
- Logical formula entailed

Prover = \dots
 $\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$



Type-checking the Prover

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}),$
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- Type of public messages
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 $\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$



Type-checking the Prover

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}),$
 $m : \text{Un},$
 \dots
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 $\text{Send}(f_{\text{tpm}}, m)$



- Type of public messages
- Logical formula entailed

Prover =



\dots
 $\text{out}(c, \text{zk}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(f_{\text{tpm}}, \text{sign}(f_{\text{tpm}}, k_I); \text{vk}(k_I), m))$

Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$$\begin{aligned} \Gamma = & \dots \\ & k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}), \\ & \dots \\ & \forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m)), \end{aligned}$$

Verifier = in(c, x).



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
assert $\text{Authenticate}(y_m)$

Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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If verification succeeds, can we assume the formula in ZK type?

Verifier = $\text{in}(c, x).$



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
assert $\text{Authenticate}(y_m)$

Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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If verification succeeds, can we assume the formula in ZK type?

In general not, the proof can come from untyped adversary!

Verifier = $\text{in}(c, x)$.



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
assert $\text{Authenticate}(y_m)$

Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$



Conceptual issue

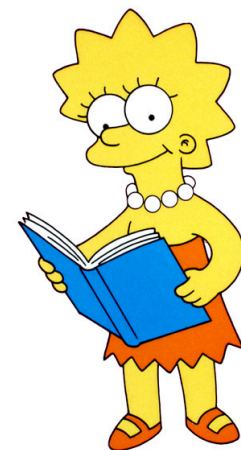
How can we know whether the zero-knowledge proof comes from an honest participant or from the adversary?!

Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$$\begin{aligned} \Gamma = & \dots \\ & k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}), \\ & \dots \\ & \forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m)), \end{aligned}$$

Verifier = $\text{in}(c, x).$
 let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
 assert $\text{Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$$\begin{aligned} \Gamma = & \dots \\ & k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}) \\ & \dots \\ & \forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f)) \rightarrow \text{OkTPM}(m)) \\ & \text{chk}(\alpha_2, \beta_1) = \alpha_1 \end{aligned}$$

The statement
instantiated with the matched
messages is valid
(by the semantics)

Verifier = in(c, x).



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
assert Authenticate(y_m)




Type-checking the Verifier

$$ZK_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$\Gamma = \dots$
 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \})$
 \dots
 $\forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f)) \rightarrow \dots)$
 $\text{chk}(\alpha_2, \beta_1) = \alpha_1$

The statement instantiated with the matched messages is valid (by the semantics)


Verifier = $\text{in}(c, x).$
 $\text{let } y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I)) \text{ then}$
 $\text{assert Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$$\Gamma = \dots$$


$$k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \})$$

$$\dots$$

$$\forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f)) \rightarrow \text{OkTPM}(m))$$

$$\text{chk}(x_s, \text{vk}(k_I)) = x_f$$

The statement
instantiated with the matched
messages is valid
(by the semantics)

Verifier = $\text{in}(c, x).$

 $\text{let } y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I)) \text{ then}$
 $\text{assert Authenticate}(y_m)$



Type-checking the Verifier

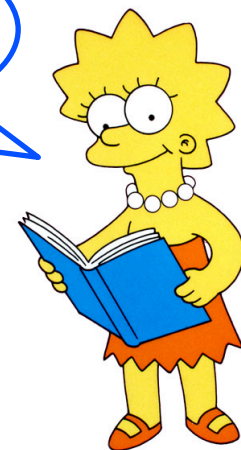
$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$\Gamma = \dots$
 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}),$
 \dots
 $\forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_s) \rightarrow \text{Authenticate}(m))),$
 $\text{chk}(x_s, \text{vk}(k_I)) = x_f$
 $x_f : \text{Private}$

The type of $\text{vk}(k_I)$ gives us the type of x_f (existentially quantified)

Verifier = $\text{in}(c, x).$

$\text{let } y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I)) \text{ then}$
 $\text{assert } \text{Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$\Gamma = \dots$
 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \})$
 \dots
 $\forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f)))$
 $\text{chk}(x_s, \text{vk}(k_I)) = x_f$
 $x_f : \text{Private}$

The prover is honest, since he knows a message of type Private!

Verifier = $\text{in}(c, x).$



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
 assert $\text{Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

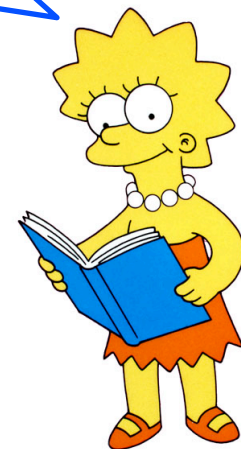
$\Gamma = \dots$
 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \})$
 \dots
 $\forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f)))$
 $\text{chk}(x_s, \text{vk}(k_I)) = x_f$
 $x_f : \text{Private}$

We can now exploit the formula in the ZK type

Verifier = $\text{in}(c, x).$



$\text{let } y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I)) \text{ then}$
 $\text{assert Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

$\Gamma = \dots$
 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}),$
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 $\text{chk}(x_s, \text{vk}(k_I)) = x_f$
 $x_f : \text{Private}$
 $\exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f)$

Verifier = $\text{in}(c, x).$
 $\text{let } y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I)) \text{ then}$
 $\text{assert } \text{Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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Verifier = $\text{in}(c, x).$
 $\text{let } y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I)) \text{ then}$
 $\text{assert } \text{Authenticate}(y_m)$



Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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 $k_I : \text{SigKey}(\langle x_f : \text{Private} \rangle \{ \text{OkTPM}(x_f) \}),$
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 $\forall m. ((\exists x_f. \text{Send}(x_f, m) \wedge \text{OkTPM}(x_f) \Rightarrow \text{Authenticate}(m)),$
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 $\exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f)$


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Type-checking the Verifier

$$\text{ZK}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1} \left(\begin{array}{l} \langle y_k : \text{VerKey}(\langle x : \text{Private} \rangle \{ \text{OkTPM}(x) \}), y_m : \text{Un} \rangle \\ \{ \exists x_f, x_s. \text{Send}(x_f, y_m) \wedge \text{OkTPM}(x_f) \} \end{array} \right)$$

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Verifier = in(c, x).



let $y_m = \text{ver}_{\text{chk}(\alpha_2, \beta_1) = \alpha_1}(x; \text{vk}(k_I))$ then
 assert $\text{Authenticate}(y_m)$



Take Home

- ▶ ZK proofs are given *dependent types* where the witnesses are *existentially quantified*



Take Home

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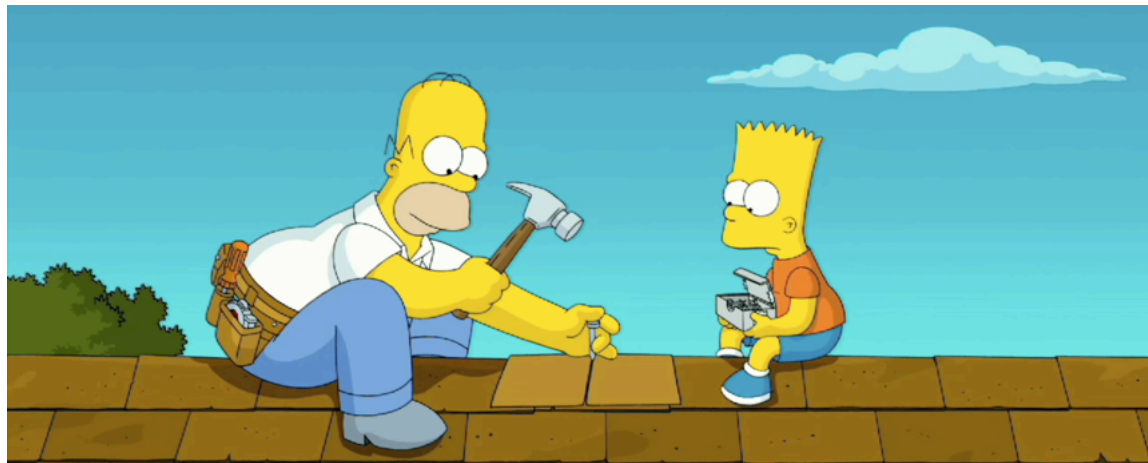
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Implementation

- ▶ Type-checker written in O’Caml (~5000 LOC)
- ▶ Uses automatic prover for discharging FOL formulas
- ▶ Extensible - very easy to add arbitrary primitives + types
- ▶ Efficient - the complete analysis of DAA takes 0.7s
- ▶ Available under the Apache License:
<http://www.infsec.cs.uni-sb.de/projects/zk-typechecker/>
- ▶ Kudos to Stefan Lorenz, Kim Pecina and Thorsten Tarrach



Ongoing Work

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[Clarkson, Chong & Myers, S&P 2008]



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THANK YOU!